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# Estimating the Maximum Radiated Electromagnetic Emissions from Complex Systems

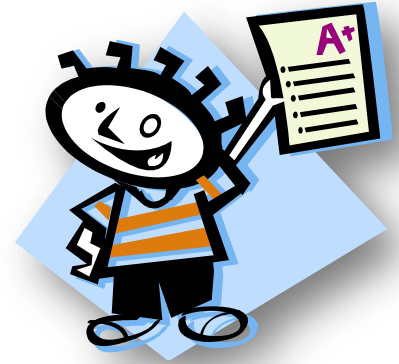
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Clemson University**



# EMC Expert Systems



- ❑ The goal is to distinguish between a good design and a bad design and identify features of a design that are likely to result in emissions or susceptibility problems.
- ❑ Existing expert system tools are capable of finding many problems that would be difficult to locate manually.

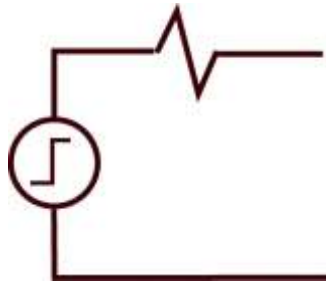
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# EMC Expert Systems

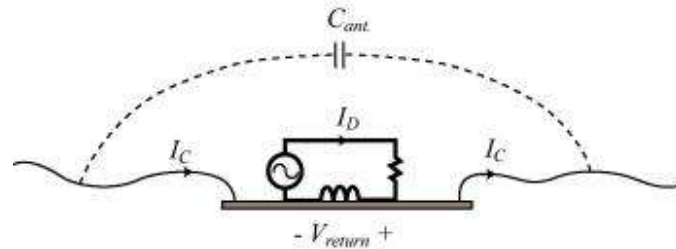
- ❑ Printed Circuit Board Layout
- ❑ Automotive EMC
- ❑ System-Level Extensions

# PCB Expert System Method

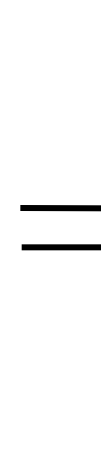
Source Model



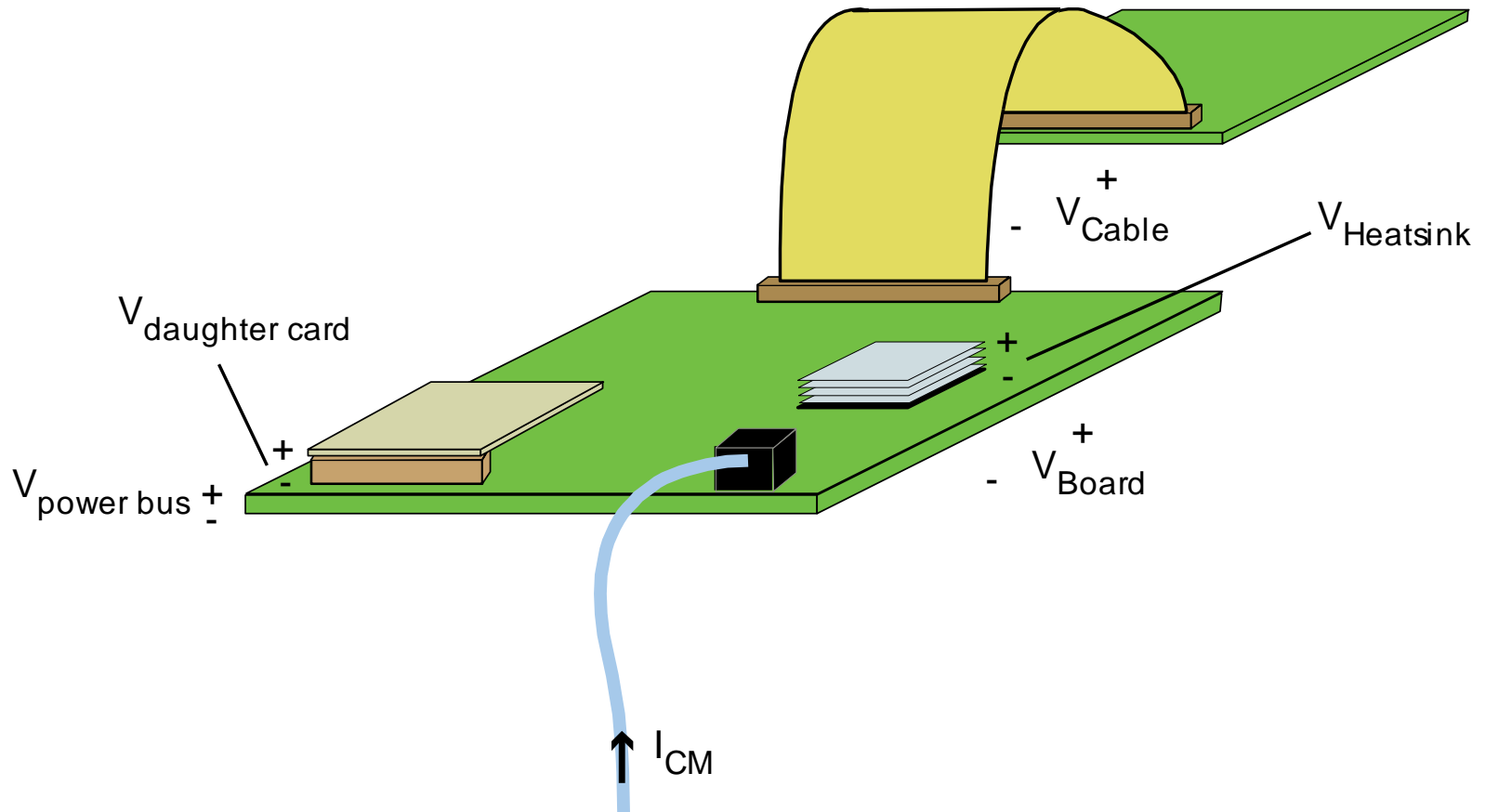
Coupling Path Model



Antenna Model



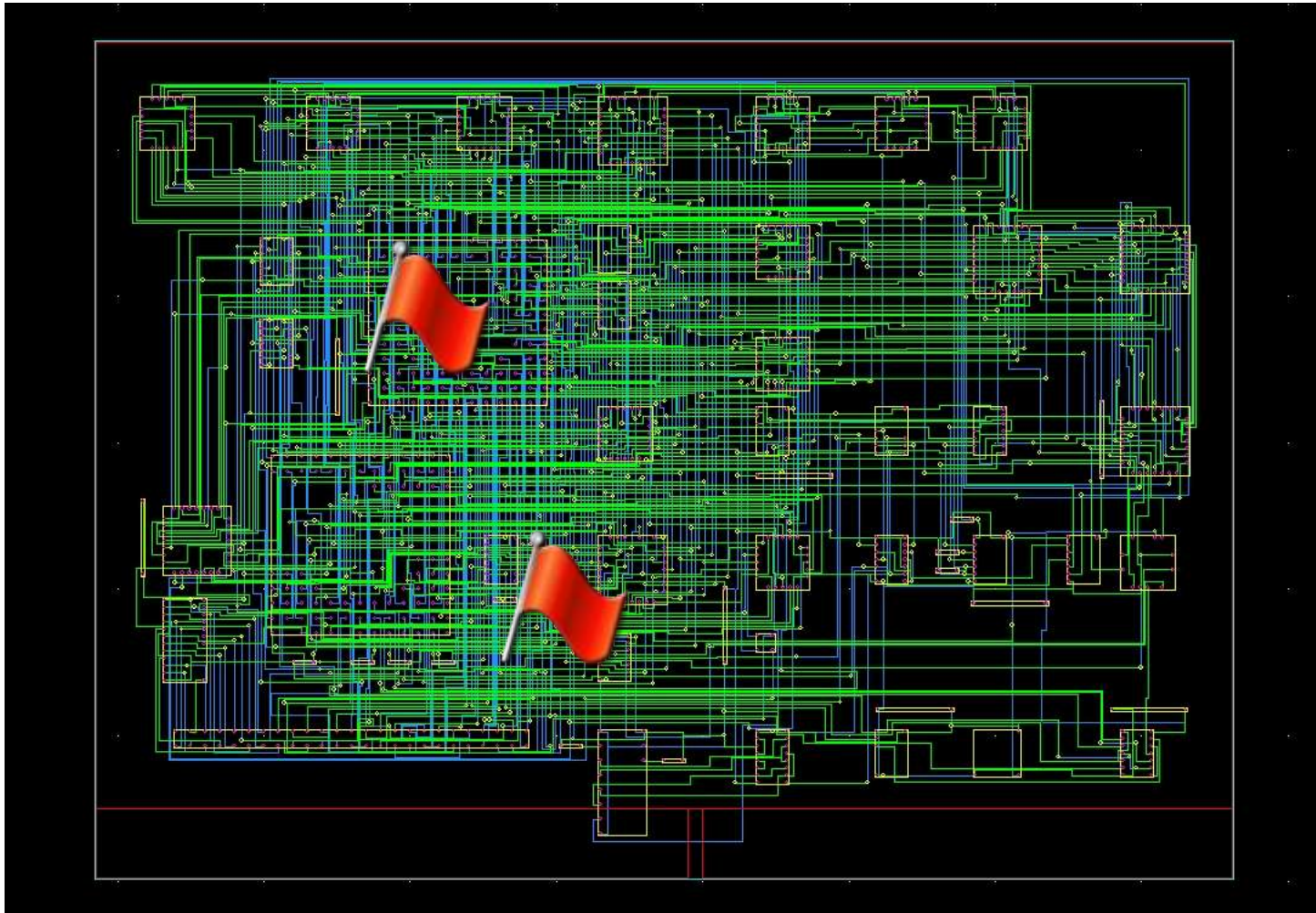
# PCB Expert System Method



# PCB Expert System Emissions Models

- ❑ Differential-Mode Radiation
- ❑ Coupling to I/O Radiation
- ❑ Voltage-Driven Common-Mode Radiation
- ❑ Current-Driven Common-Mode Radiation
- ❑ Power Bus Radiation

# Algorithms Locate Hard-to-Find Problems



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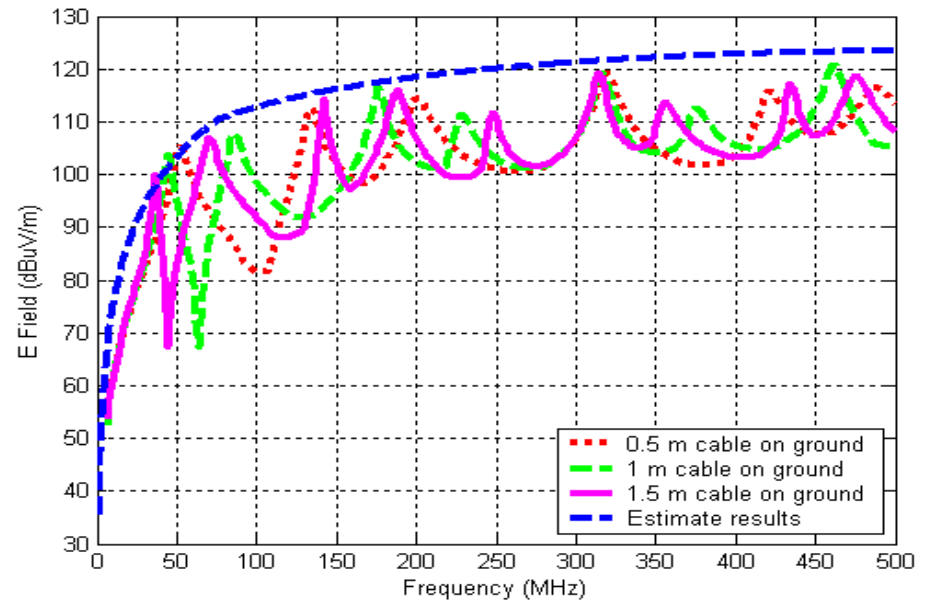
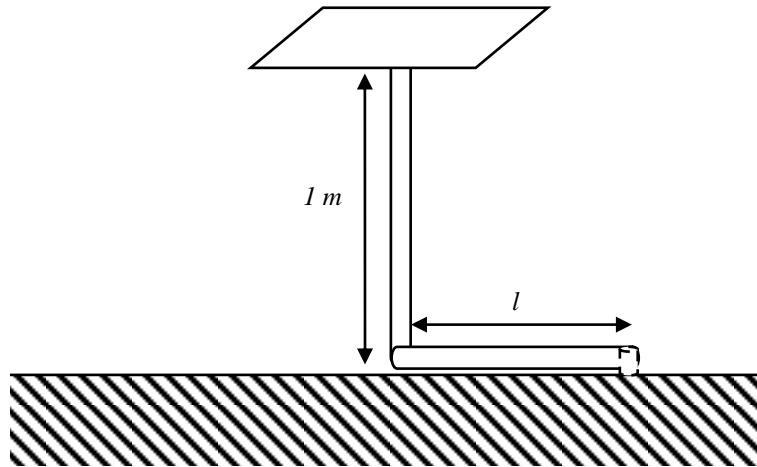
**Expert System Algorithms are constantly asking the question,**



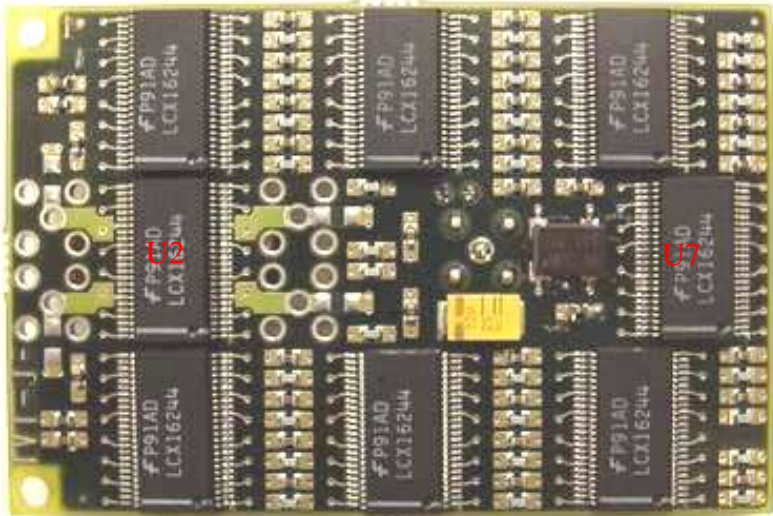
**What's the worst that could happen?**



# Effect of Extended Cable on Ground

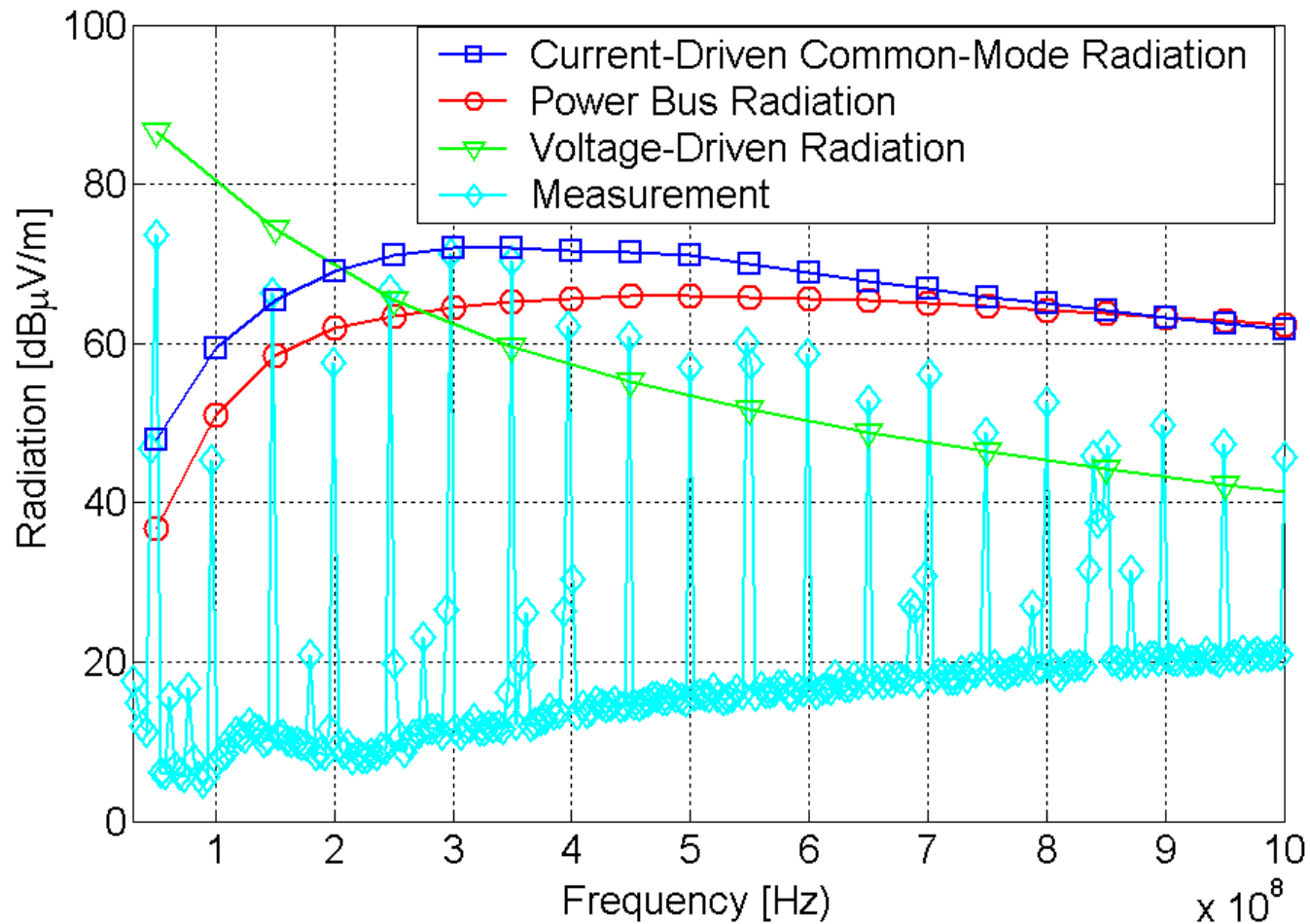


# Board Analysis using Expert System Algorithms



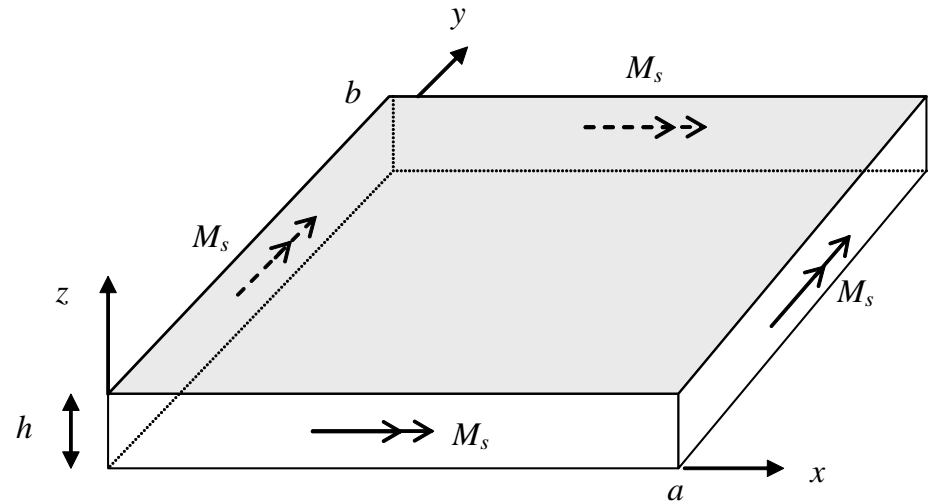
- 8 clock buffers
- 28 load capacitors
- 32 decoupling capacitors
- Clocked at 50 MHz
- No heatsink
- Size: 3" by 2", 6 layers
- Powered with one cable

# Measurement vs. Calculation: 1-nF Load



# Power Bus Radiation Model

$$Q(f) = \left( \frac{1}{Q_d} + \frac{1}{Q_c} + \frac{1}{Q_{\text{comp}}} \right)^{-1}$$



$$|E| = \frac{120I_i}{\epsilon_r \min(a, b)} \times \frac{h}{r} \times Q(f)$$

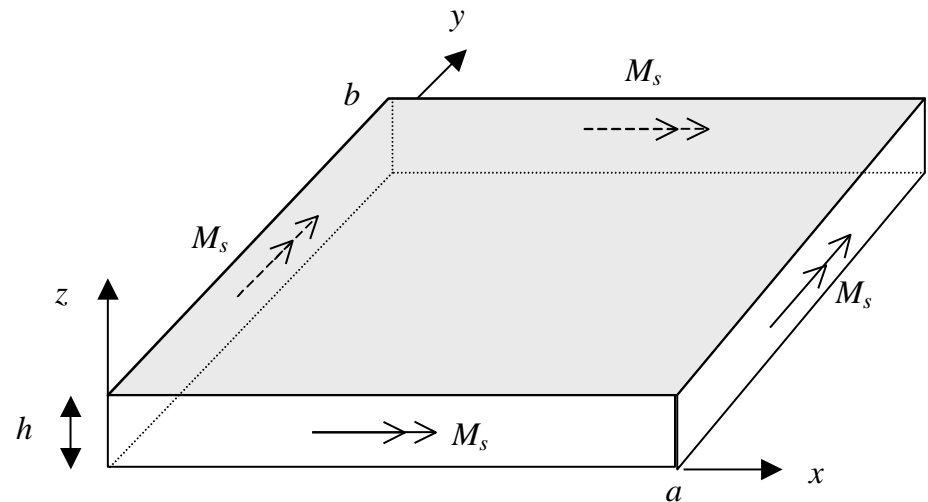
H. Shim and T. Hubing, "Estimating radiated emissions from the power planes in a populated printed circuit board," *IEEE Trans. on Electromagnetic Compatibility*, vol. 48, no. 1, Feb. 2006.

# Maximum Power Bus Radiation

$$|E| = f(r, \theta, \varphi, \epsilon_r, h, L, W, \omega) \times V(0,0)$$

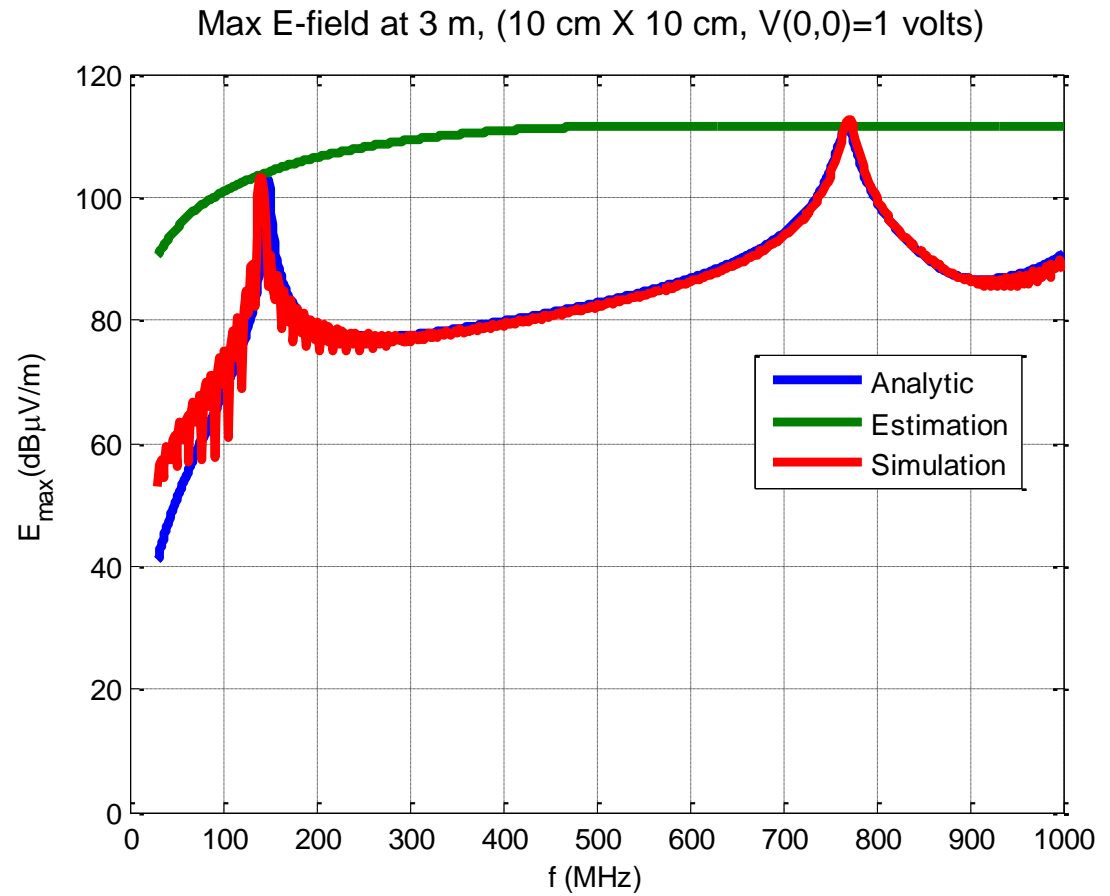
$$\text{board\_size\_factor} \equiv \begin{cases} \sin\left(\frac{2\pi \ell_{\text{board}}}{\lambda}\right) & \text{when } \ell_{\text{board}} \leq \frac{\lambda}{4} \\ 1.0 & \text{otherwise} \end{cases}$$

$$|E|_{\text{max}} = f_{\text{max}} \times V(0,0) \times \text{board\_size\_factor}$$



# Maximum Power Bus Radiation

$$|E|_{\max} = f_{\max} \times V(0,0) \times \text{board\_size\_factor}$$

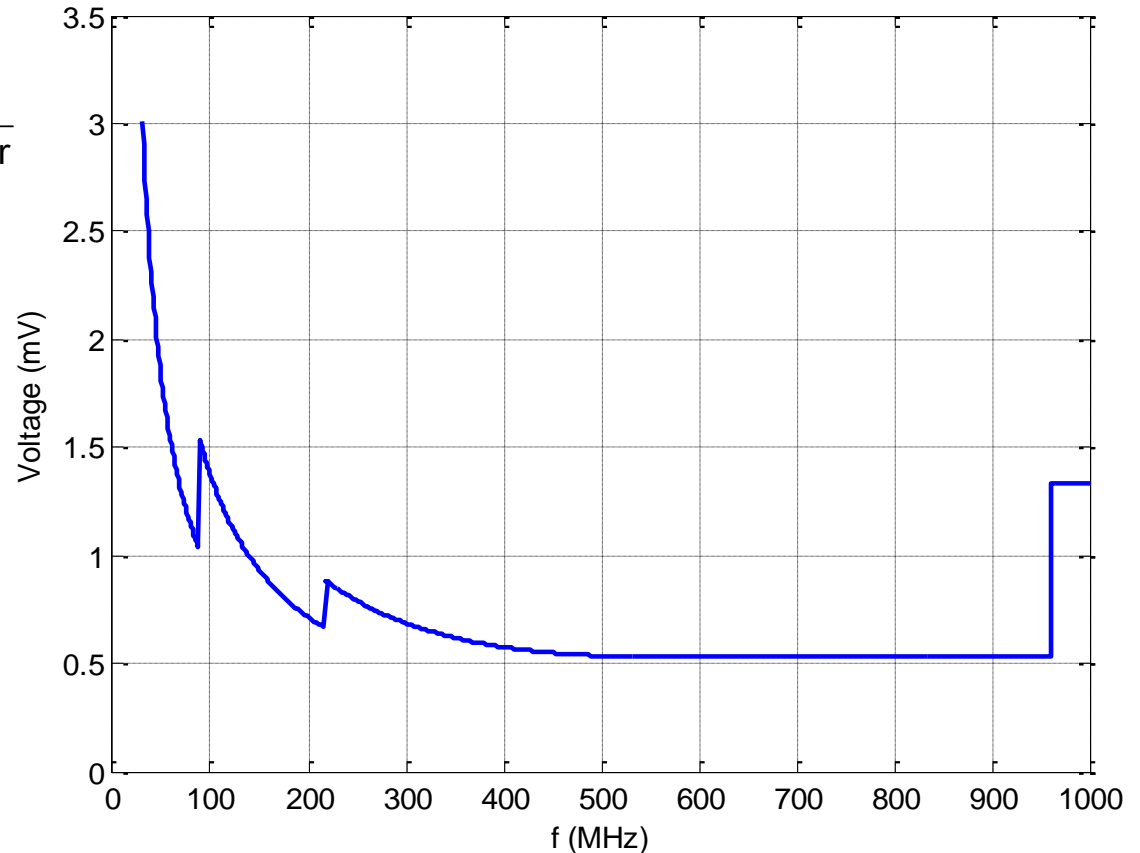


# Minimum Power Bus Voltage

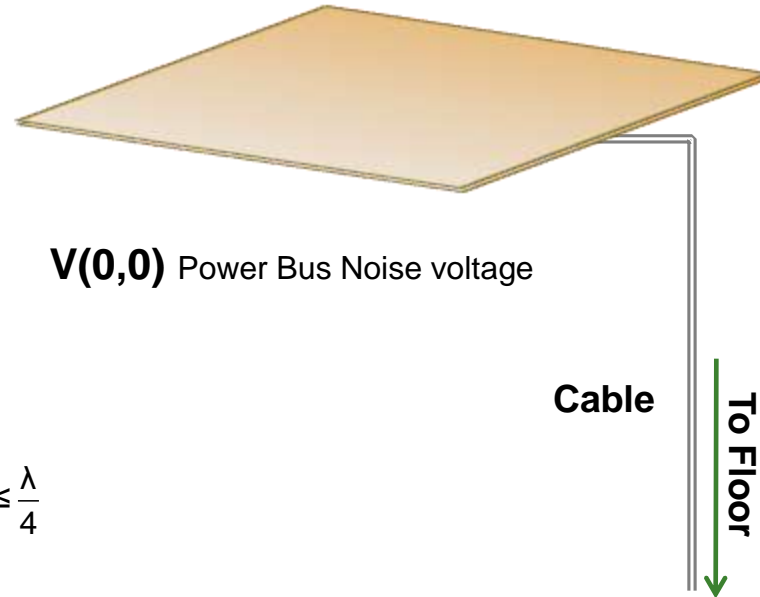
Expert System Field Calculation  
Performed in Reverse

Minimum voltage required to generate fields  
exceeding the FCC Class B limit

$$V(0.0)_{\min} = \frac{|E|_{\text{FCC}}}{f_{\max} \times \text{board\_size\_factor}}$$



# Minimum Power Bus Voltage (Board w/Cable)



$$|E| = 20 \times I_{0(\max)} \times f_{\max}(\theta, k) = 20 \times \frac{V(0,0)}{37 \text{ ohm}} \times 2.76$$

$$\text{cable\_rad\_factor} \equiv \begin{cases} \sin\left(\frac{2\pi l_{\text{cable}}}{\lambda}\right) & \text{when } l_{\text{cable}} \leq \frac{\lambda}{4} \\ 1.0 & \text{otherwise} \end{cases}$$

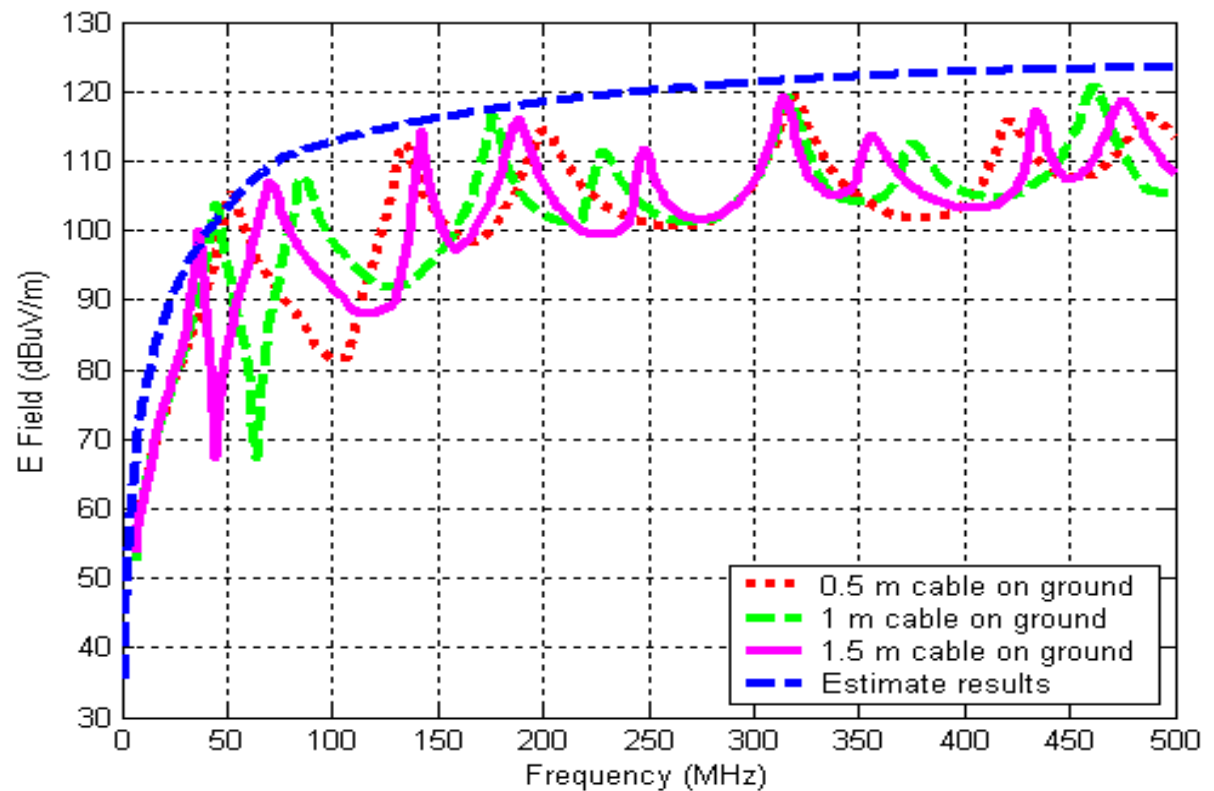
$$\text{board\_size\_factor} \equiv \begin{cases} \sin\left(\frac{2\pi l_{\text{board}}}{\lambda}\right) & \text{when } l_{\text{board}} \leq \frac{\lambda}{4} \\ 1.0 & \text{otherwise} \end{cases}$$

$$|E|_{\min} = |E| \times \text{cable\_rad\_factor} \times \text{board\_size\_factor}$$



# Minimum Power Bus Voltage (Board w/Cable)

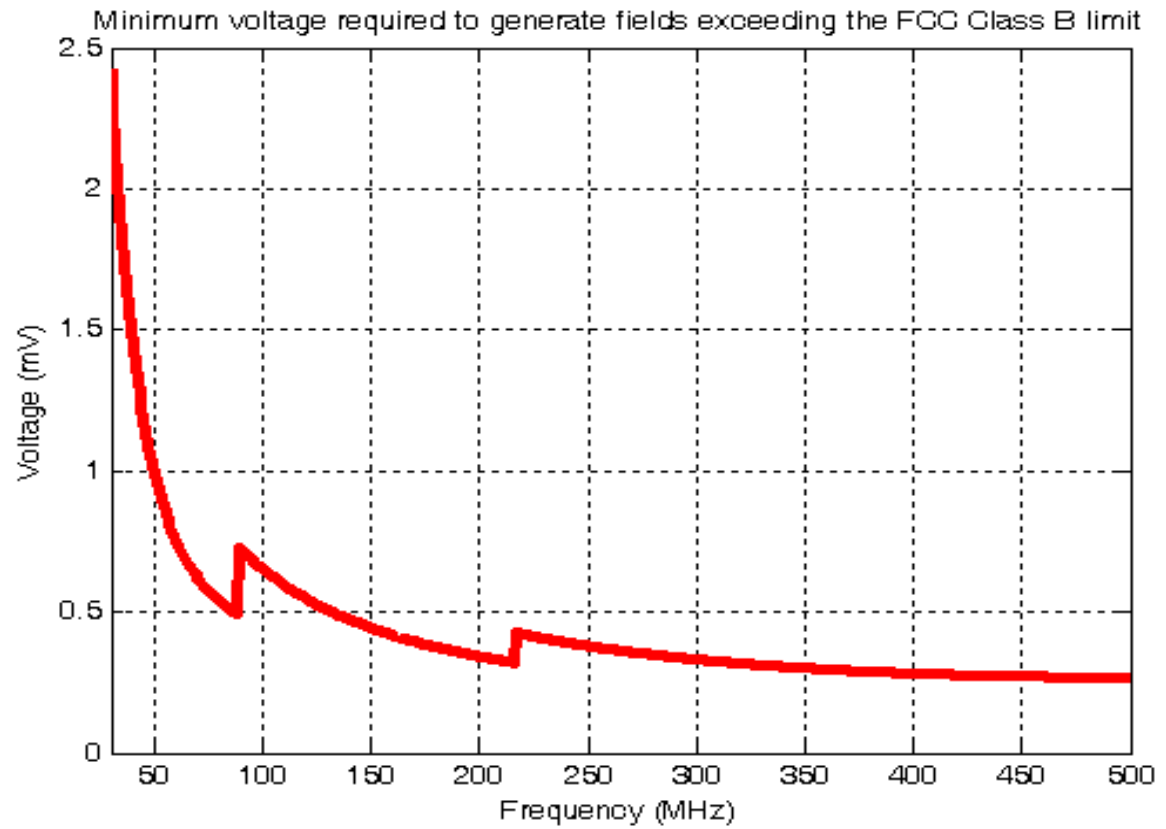
$$|E|_{\min} = |E| \times \text{cable\_rad\_factor} \times \text{board\_size\_factor}$$



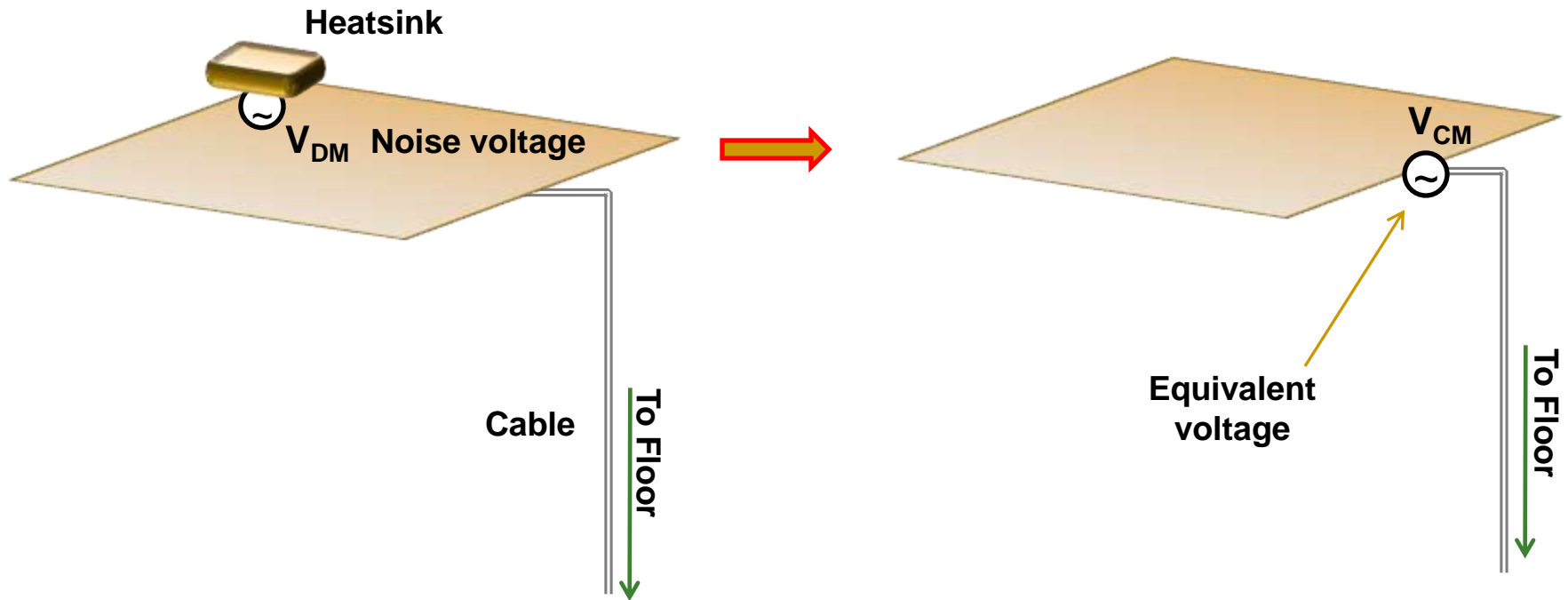
# Minimum Power Bus Voltage (Board w/Cable)

Expert System Field Calculation  
Performed in Reverse

$$V_{\min} = \frac{|E|_{\max}}{\text{cable\_rad\_factor} \times \text{board\_size\_factor}} \times 37 \text{ ohm} / 20 \times 2.76$$



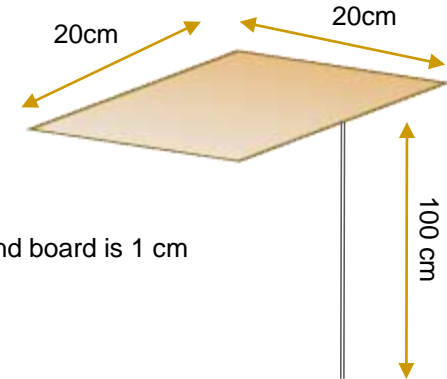
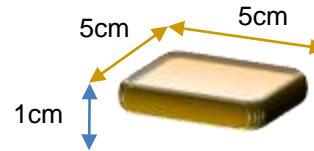
# IC-Heatsink to Cable Coupling



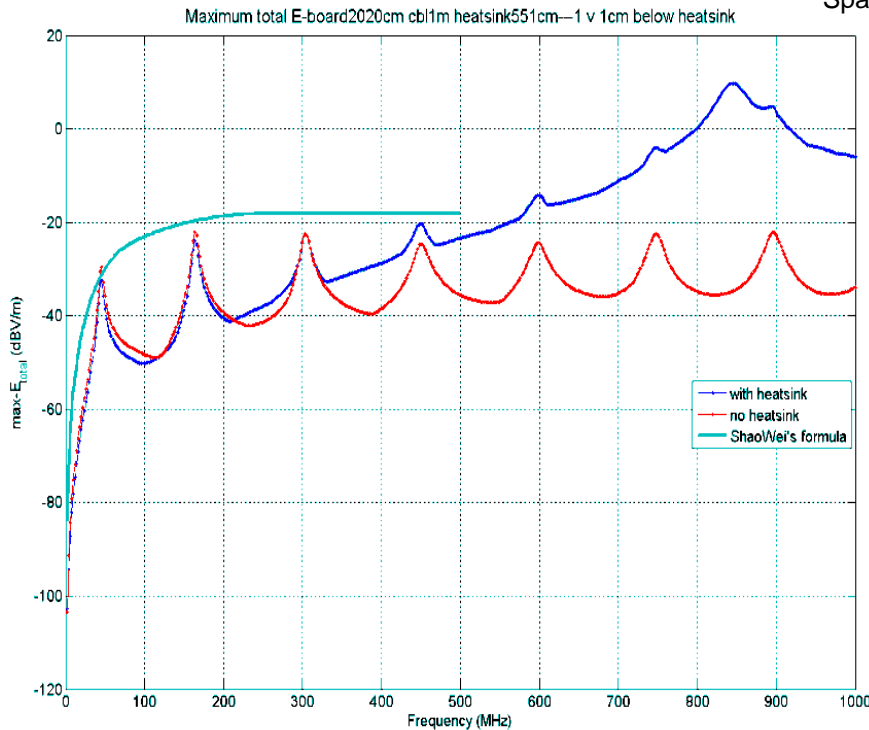
$$V_{CM} = \frac{C_{\text{heatsink}}}{C_{\text{board}}} V_{DM}$$

$$V_{DM} = 0.2234 \frac{C_{\text{board}}}{C_{\text{heatsink}}} \times \frac{r}{F_{\text{board}} F_{\text{cable}}} \times |E_{\text{max}}|$$

# IC-Heatsink to Cable Coupling



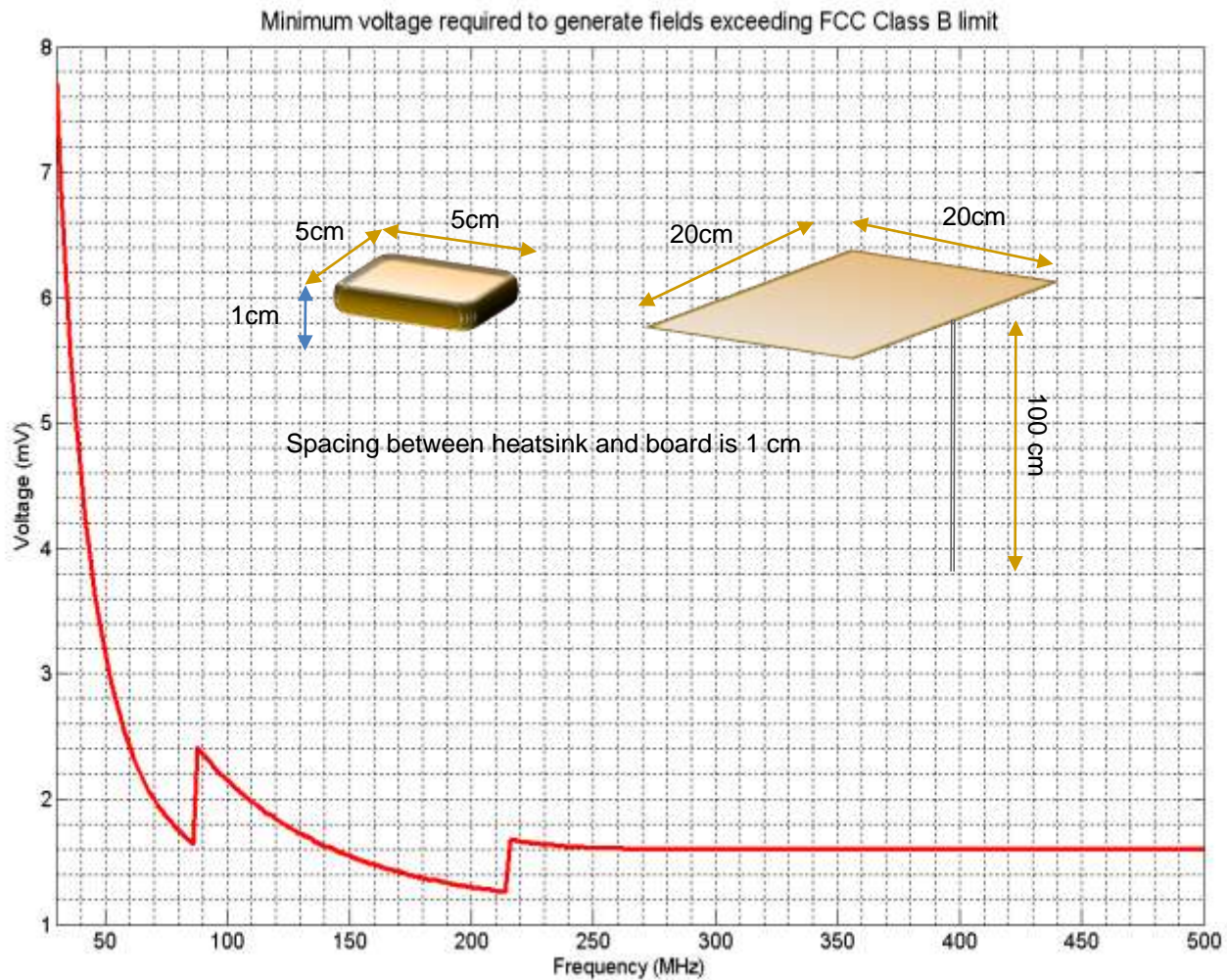
Spacing between heatsink and board is 1 cm



$$C_{heatsink} = 0.43 \text{ pF}$$

$$C_{board} = 5.14 \text{ pF}$$

# IC-Heatsink to Cable Coupling



# Conclusions

- ❑ EMC expert systems employ “maximum radiated emissions” algorithms that estimate the worst-case emission based on the information available about the system.
- ❑ These algorithms are useful for EMC design analysis, which is nearly always performed with incomplete or approximate data.
- ❑ These algorithms can be a useful for trouble shooting circuit boards because voltages and currents measured on the board can be related to possible emissions sources.