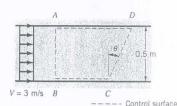
4.71 Water flows through the 2-m-wide rectangular channel shown in Fig. P4.71 with a uniform velocity of 3 m/s. (a) Directly integrate Eq. 4.16 with b=1 to determine the mass flowrate (kg/s) across section CD of the control volume. (b) Repeat part (a) with $b=1/\rho$, where ρ is the density. Explain the physical interpretation of the answer to part (b).

b) With b= 1/p Eq. (1) becomes



(1)

MFIGURE P4.7/

a)
$$\dot{B}_{out} = \int_{csout} \rho b \, \vec{V} \cdot \hat{n} \, dA$$

With $b = l$ and $\vec{V} \cdot \hat{n} = V \cos \theta$ this becomes

 $\dot{B}_{out} = \int_{cb} \rho V \cos \theta \, dA = \rho V \cos \theta \int_{cb} dA$
 $= \rho V \cos \theta \, A_{cb}$, where $A_{cb} = l (2m)$
 $= (\frac{0.5 \, m}{\cos \theta})(2m)$
 $= (\frac{l}{\cos \theta}) m^2$

Thus, with
$$V=3m/s$$
,
$$\dot{B}_{out} = (3\frac{m}{s})\cos\theta \left(\frac{1}{\cos\theta}\right)m^2(999\frac{kq}{m^3}) = 3000\frac{kq}{s}$$

$$\dot{B}_{out} = \int \vec{V} \cdot \hat{n} \, dA = \int V \cos \theta \, dA = V \cos \theta \, A_{cD}$$

$$= (3 \frac{m}{s}) \cos \theta \, \left(\frac{1}{\cos \theta}\right) m^2 = \underline{3.00 \frac{m^3}{s}}$$

$$With \ b = 1/\rho = \frac{1}{(\frac{mass}{vol})} = \frac{vol}{mass} \ it \ follows \ that "B = volume"$$

$$(i.e., b = \frac{B}{mass}) \ so \ that \ \int \vec{V} \cdot \hat{n} \, dA = \dot{B}_{out} \ represents \ the \ volume$$

$$flowrate \ (m^3/s) \ from \ the \ control \ volume.$$