

5.110

5.110 The hydroelectric turbine shown in Fig. P5.110 passes 8 million gal/min across a head of 600 ft. What is the maximum amount of power output possible? Why will the actual amount be less?

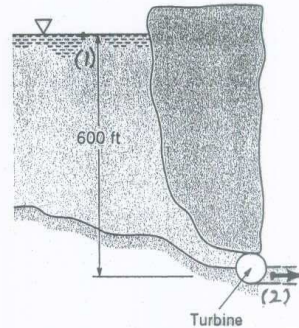


FIGURE P5.110

From the energy equation

$$\frac{p_1}{\rho} + z_1 + \frac{V_1^2}{2g} + h_s - h_L = \frac{p_2}{\rho} + z_2 + \frac{V_2^2}{2g}$$

where $p_1 = 0$, $p_2 = 0$, and $V_1 = 0$.

Thus,

$$h_s = (z_2 - z_1) + h_L + \frac{V_2^2}{2g}$$

And, the power is given by

$$\dot{W}_{\text{turb}} = \rho Q h = \rho Q \left[(z_2 - z_1) + h_L + \frac{V_2^2}{2g} \right]$$

The maximum power would occur if there were no losses ($h_L = 0$) and negligible kinetic energy at the exit ($V_2 \approx 0$; large diameter outlet).

Thus,

$$\begin{aligned} \dot{W}_{\text{turb max}} &= \rho Q (z_2 - z_1) = 62.4 \frac{\text{lb}}{\text{ft}^3} (8 \times 10^6 \frac{\text{gal}}{\text{min}}) \left(\frac{1 \text{ min}}{60 \text{ s}} \right) \left(\frac{1 \text{ ft}^3}{7.48 \text{ gal}} \right) (600 \text{ ft}) \\ &= 6.67 \times 10^8 \frac{\text{ft} \cdot \text{lb}}{\text{s}} \left(\frac{1 \text{ hp}}{550 \frac{\text{ft} \cdot \text{lb}}{\text{s}}} \right) = \underline{\underline{-1.21 \times 10^6 \text{ hp}}} \end{aligned}$$

The minus sign is associated with power out.

The actual power will be less by amounts corresponding to loss and exit kinetic energy.