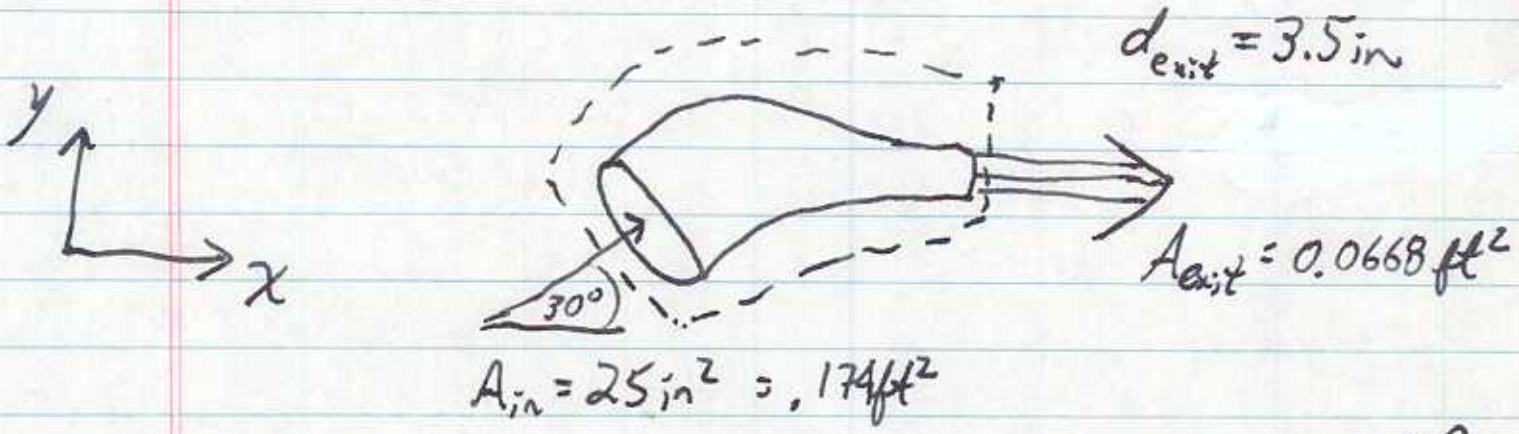


MYO 5.36

Jet-Ski Problem



Thrust = -300 lb

$P_{in} = P_{exit} = 0$

$\Sigma F_{x, \text{ contents of c.v.}} = +300 \text{ lb}$

$$\Sigma F_x = \frac{\partial}{\partial t} \int_{c.v.} \rho \vec{v} dV + \int_{c.s.} \vec{v} \rho \vec{v} \cdot \vec{n} dA$$

steady flow

$$300 \text{ lb} = v_x \rho \vec{v} \cdot \vec{n} \int_{c.s.} dA$$

Assuming uniform flow at inlets/outlets

MYO 5.36 continued

$$300 = \rho \left[(V_x \hat{V} \cdot \hat{n} A)_{\text{inlet}} + (V_x \hat{V} \cdot \hat{n} A)_{\text{exit}} \right]$$

$$\left[\frac{300 \text{ lb}}{\rho} = V_{\text{in}} (\cos 30^\circ) (-V_{\text{in}}) A_{\text{in}} + V_{\text{exit}} V_{\text{exit}} A_{\text{exit}} \right]$$

Two unknowns: V_{in} , V_{exit} .

Need a 2nd Equation

Conservation of Mass $\Rightarrow V_{\text{in}} A_{\text{in}} = V_{\text{exit}} A_{\text{exit}}$

$$V_{\text{exit}} = V_{\text{in}} \frac{A_{\text{in}}}{A_{\text{exit}}}$$

$$\frac{300 \text{ lb}}{\rho} = -\cos 30^\circ V_{\text{in}}^2 A_{\text{in}} + V_{\text{in}}^2 \left(\frac{A_{\text{in}}}{A_{\text{exit}}} \right)^2 A_{\text{exit}}$$

$$\frac{300 \text{ lb}}{1.94 \frac{\text{slugs}}{\text{ft}^3}} = -.866 V_{\text{in}}^2 (.17 \text{ ft}^2) + (V_{\text{in}}^2) (.453 \text{ ft}^2)$$

$$V_{\text{in}} = 22.6 \text{ ft/s}$$

$$\dot{V} = A_{\text{in}} V_{\text{in}} = 3.93 \text{ ft}^3/\text{s}$$