

# **TRUST-BASED CONTROL AND MOTION PLANNING FOR MULTI-ROBOT SYSTEMS WITH A HUMAN-IN-THE-LOOP**

**Yue Wang, Ph.D.**

**Warren H. Owen - Duke Energy Assistant Professor of Engineering**

**Interdisciplinary & Intelligent Research (I<sup>2</sup>R) Laboratory**

**Department of Mechanical Engineering, Clemson University**



**ICRA2017**

May 29 - June 3, 2017 • Singapore





**Background and Motivation**



**Computational Trust Models**



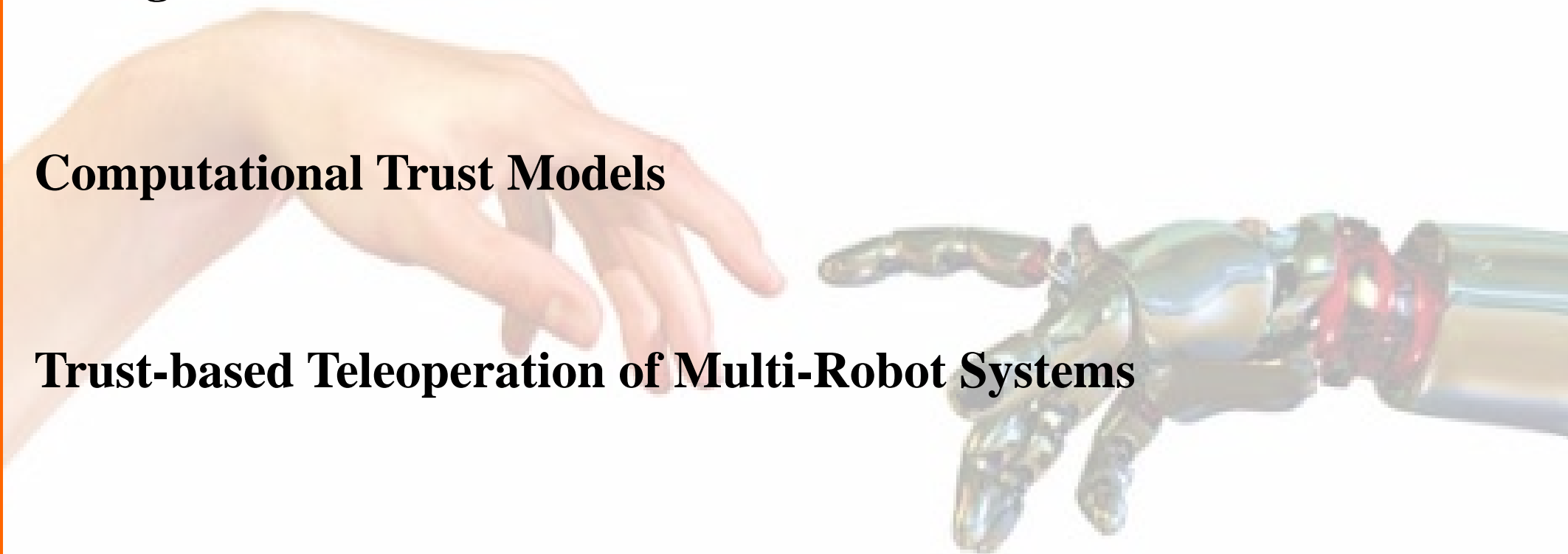
**Trust-based Teleoperation of Multi-Robot Systems**



**Trust-based Multi-Robot Symbolic Motion Planning**



**Conclusions**





## **Background and Motivation**



## **Computational Trust Models**



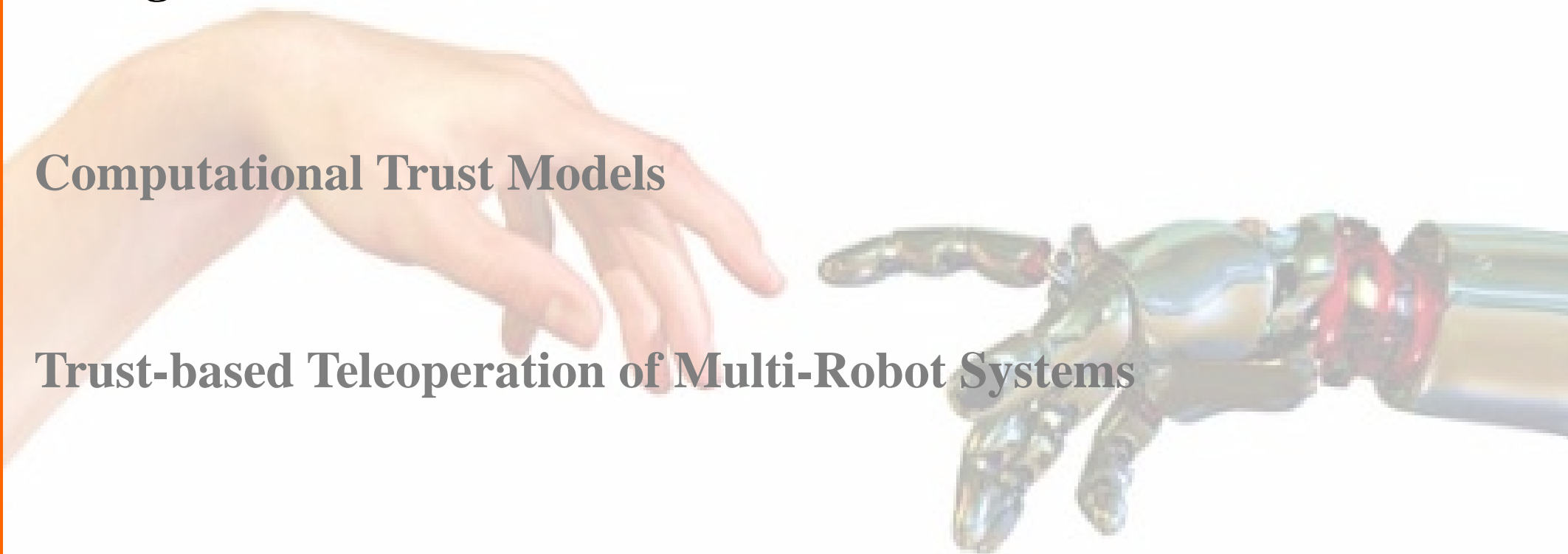
## **Trust-based Teleoperation of Multi-Robot Systems**



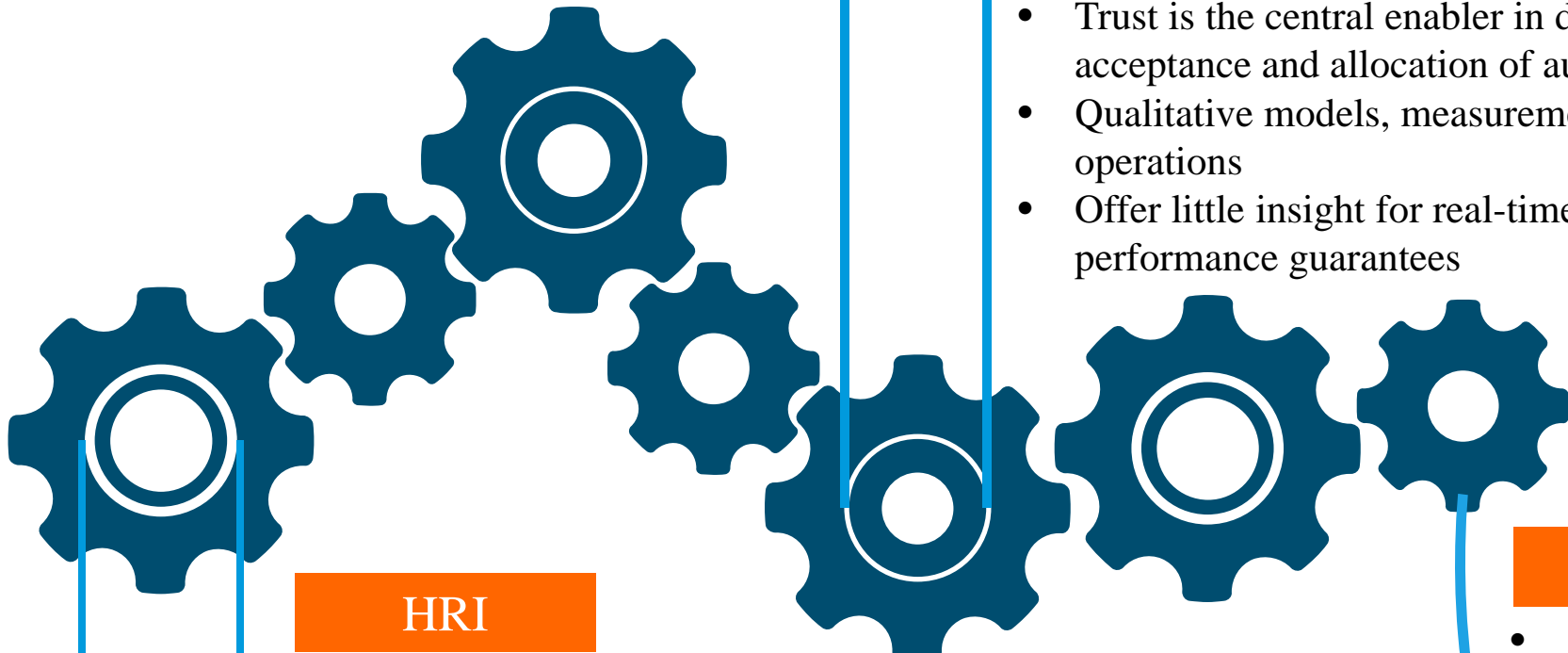
## **Trust-based Multi-Robot Symbolic Motion Planning**



## **Conclusions**



# Background & Motivation



## HRI

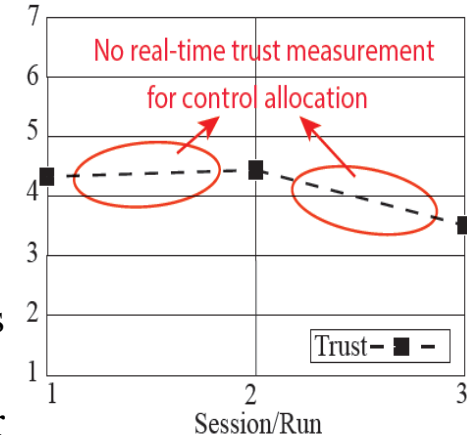
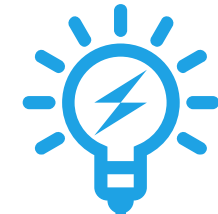
- Human-machine interface (HMI) design
- Lack understanding of the dynamic interaction for real-time robotic operations in complex and uncertain environments
- Lack system-level performance guarantees and verification
- Human-robot interaction (HRI) in multi-robot systems is especially challenging

## Trust

- Trust is the central enabler in determining human's acceptance and allocation of automation
- Qualitative models, measurements before and after operations
- Offer little insight for real-time robotic operations and performance guarantees

## Novelty

- Social/Psychological/Physical HRI for real-time robotic operations
- Quantitative analysis
- Embed human factors analysis into control theory, decision theory, and robot motion planning



Subjective Trust Measurement



## **Background and Motivation**



## **Computational Trust Models**



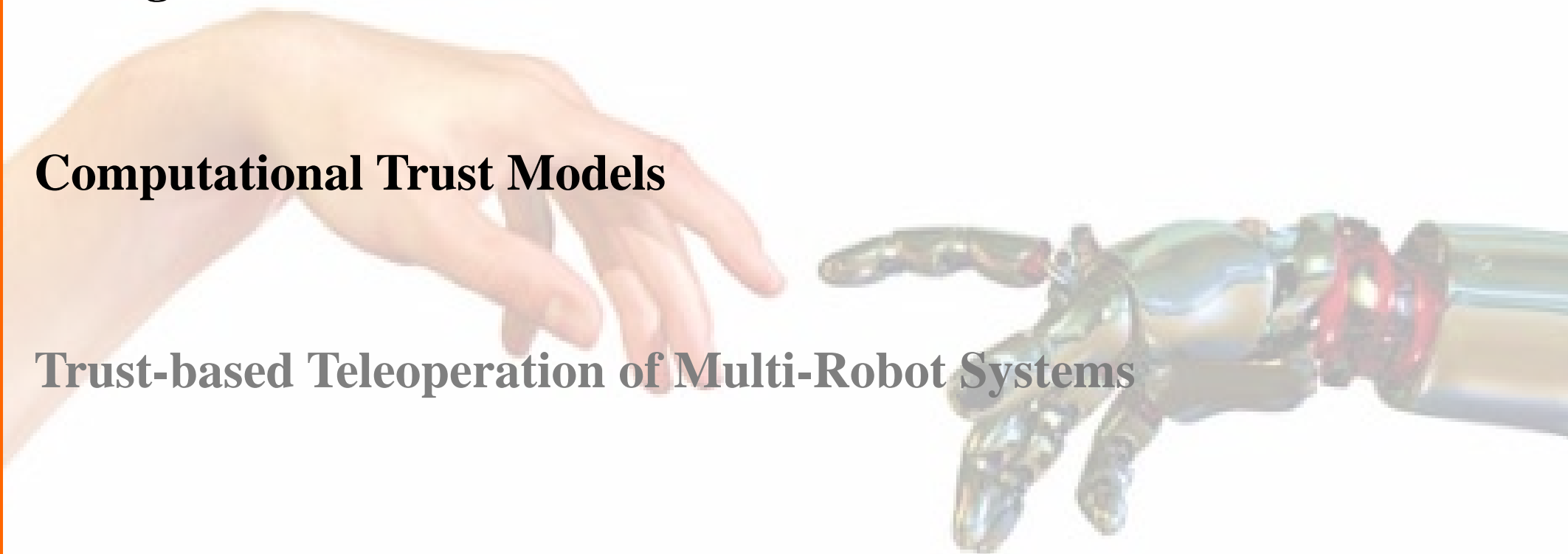
## **Trust-based Teleoperation of Multi-Robot Systems**



## **Trust-based Multi-Robot Symbolic Motion Planning**

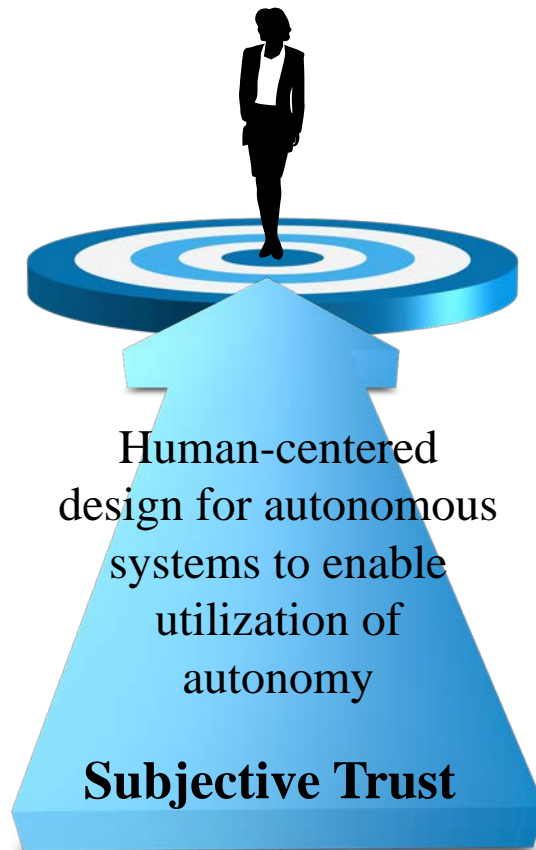


## **Conclusions**



# Computational Trust Models

Trust - “the attitude that an agent will help achieve an individual’s goals in a situation characterized by uncertainty and vulnerability.” [Lee & See, *Human Factors*, 2004]

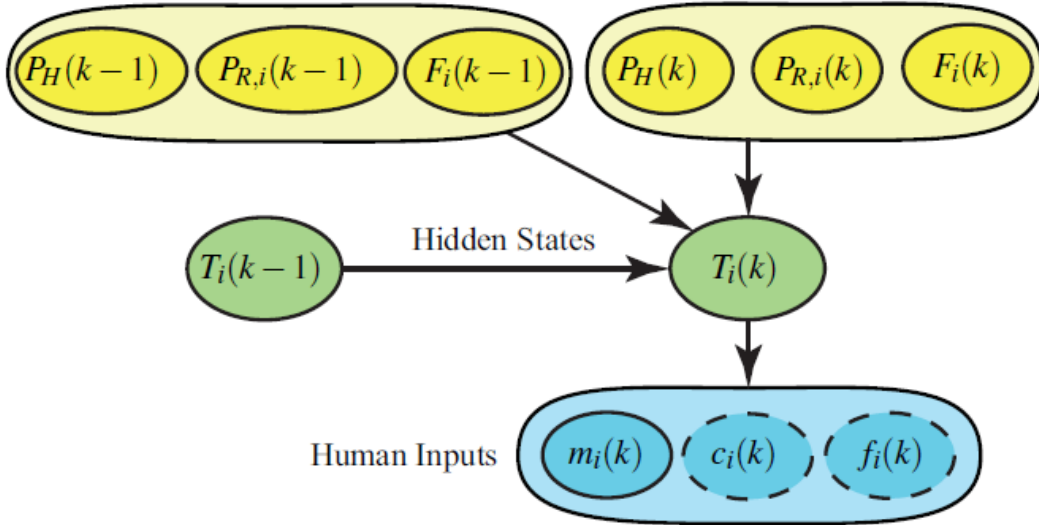


## Our Trust Models

- Time-series trust model [Wang et. al. Springer 2014; B. Sadrfaridpour et. al. Springer 2015; Rahman et. al. DSCC 2015a; Saeidi & Wang, CDC 2015; Saeidi et. al. ACC 2016; Sadrfaridpour et. al. CASE 2016; Rahman et. al. CASE 2016a; Spencer et. al., IROS 2016; Mahani & Wang, DSCC 2016; Saeidi et. al., T-RO 2017]
- Dynamic Bayesian Network (DBN) trust model [Wang et. al., ACM TiiS 2017]
- Robot-to-human trust model [Walker et. al. MSCI 2015; Rahman et. al. CASE 2016a]
- Mutual trust model [Wang et. al. ACC 2015, CPS 2015; Wang & Zhang ed., Springer 2017]
- RoboTrust for multi-robot systems [Saeidi et. al., IROS 2017]

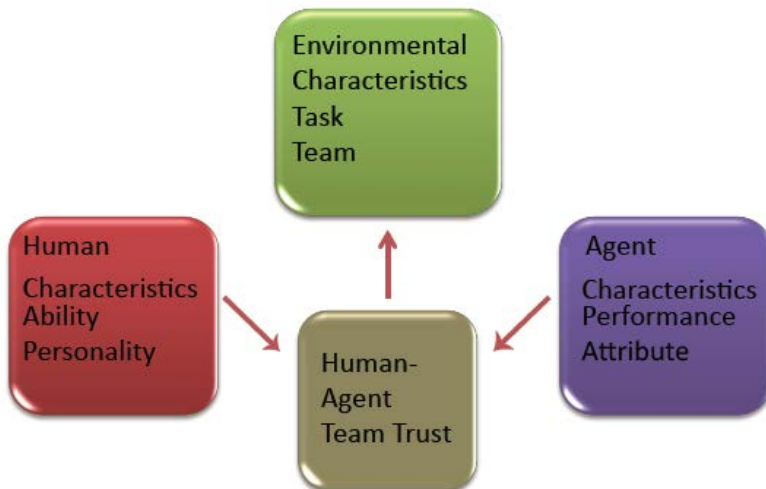
# DBN Trust Models

[Wang et. al., ACM Tiis 2017]

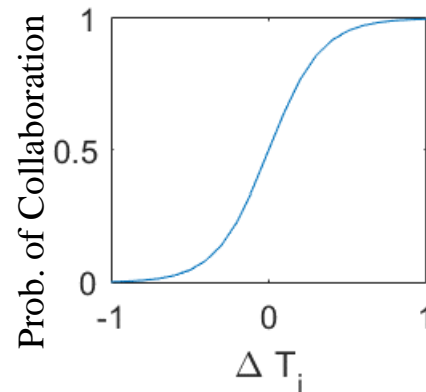


$$\begin{aligned} & \text{Prob}(T_i(t) | P_{R,i}(1:t), P_H(1:t), F_i(1:t), m_i(1:t), c_i(1:t), f_i(1:t), T_i(0)) \\ &= \text{bel}(T_i(t)) = \frac{\int \overline{\text{bel}}(T_i(t), T_i(t-1)) dT_i(t-1)}{\int \int \overline{\text{bel}}(T_i(t), T_i(t-1)) dT_i(t-1) dT_i(t)} \\ & \overline{\text{bel}}(T_i(t), T_i(t-1)) \\ &= \text{Prob}(m_i(t) | T_i(t), T_i(t-1)) \text{Prob}(c_i(t) | T_i(t), T_i(t-1)) \text{Prob}(f_i(t) | T_i(t)) \cdot \\ & \text{Prob}(T_i(t) | T_i(t-1), P_{R,i}(t), P_{R,i}(t-1), P_H(t), P_H(t-1), F_i(t), F_i(t-1)) \text{bel}(T_i(t-1)) \\ & \text{Prob}(T_i(t) | T_i(t-1), P_{R,i}(t), P_{R,i}(t-1), P_H(t), P_H(t-1), F_i(t), F_i(t-1)) \\ &= \mathcal{N}(T_i(t); \bar{T}_i(t), \sigma_i(t)), \\ & \text{where } \bar{T}_i(t) = AT_i(t-1) + B_1 P_{R,i}(t) - B_2 P_{R,i}(t-1) + C_1 P_H(t) - C_2 P_H(t-1) \\ & \quad + D_1 F_i(t) - D_2 F_i(t-1). \\ & \text{Prob}(m_i(t) = 1 | T_i(t), T_i(t-1)) = (1 + \exp(-(\omega_1 T_i(t) - \omega_2 T_i(t-1))))^{-1} \end{aligned}$$

## Main Factors



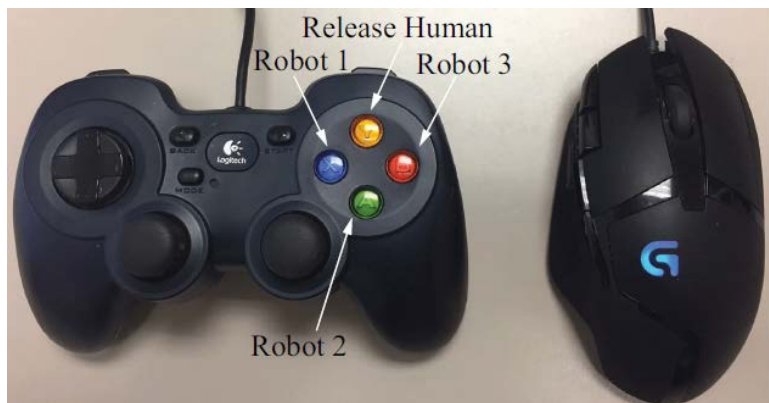
## Autonomy Allocation



- Xu & Dudek. “OPTIMo: Online probabilistic trust inference model for asymmetric human-robot collaborations”, In *Proc. ACM/IEEE Int. Conf. HRI*, 2015.
- Lee & Moray, “Trust, control strategy, and allocation of function in human-machine systems”, *Ergonomics*, 1992.
- Hancock, et al. “A meta-analysis of factors affecting trust in human-robot interaction”, *Human Factors*, 2011.
- Hoff & Bashir, “Trust in Automation: Integrating Empirical Evidence on Factors that Influence Trust”, *Human Factors*, 2014



# DBN Trust Models



**Trust Change?**

**Robot 1**  Lose  Unchange  Gain

**Robot 2**  Lose  Unchange  Gain

**Robot 3**  Lose  Unchange  Gain

**Confirm**

**What is your degree of trust in the robot right now?**

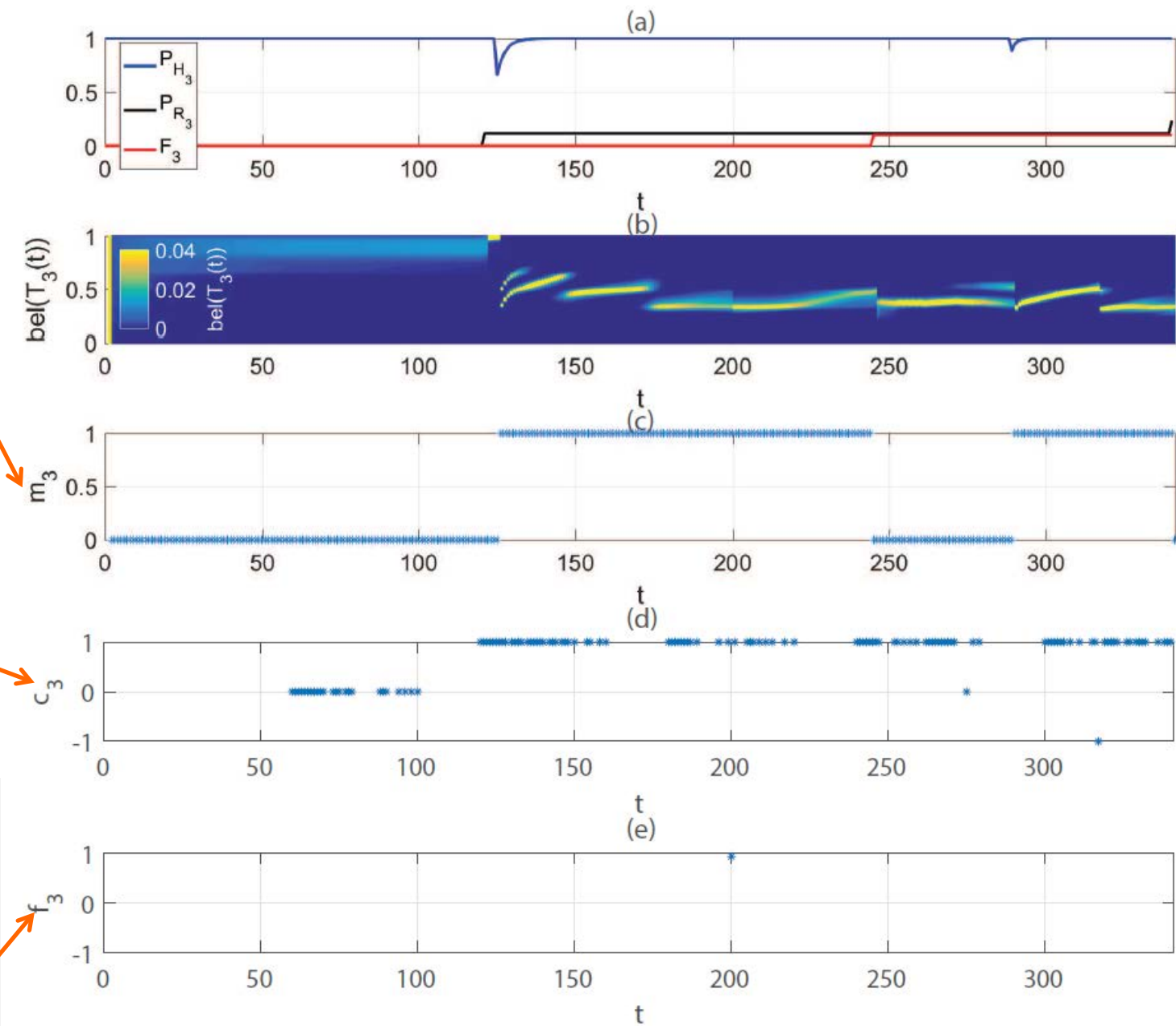
**Robot 1**

**Robot 2**

**Robot 3**

full distrust    distrust    neutral    trust    full trust

**Confirm**



Real-time trust computation: (a) human, robot performance, fault, (b) trust belief, (c) human collaboration, (d) trust change, and (e) direct subjective trust measure





## **Background and Motivation**



## **Computational Trust Models**



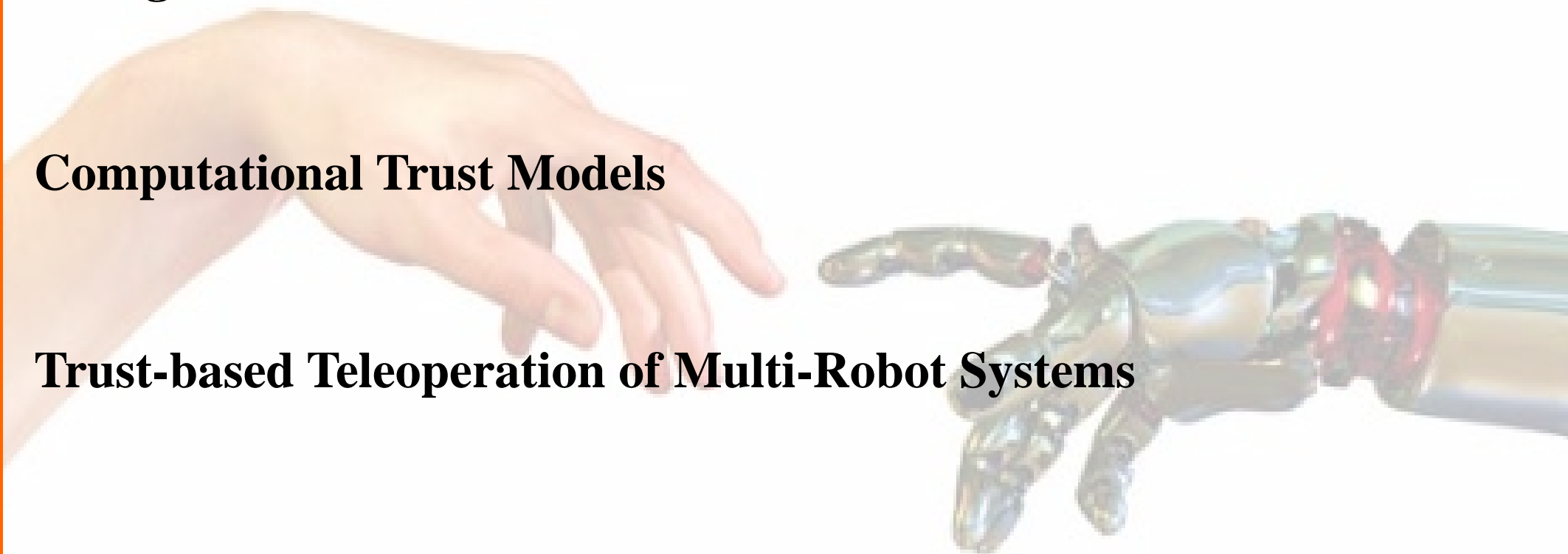
## **Trust-based Teleoperation of Multi-Robot Systems**



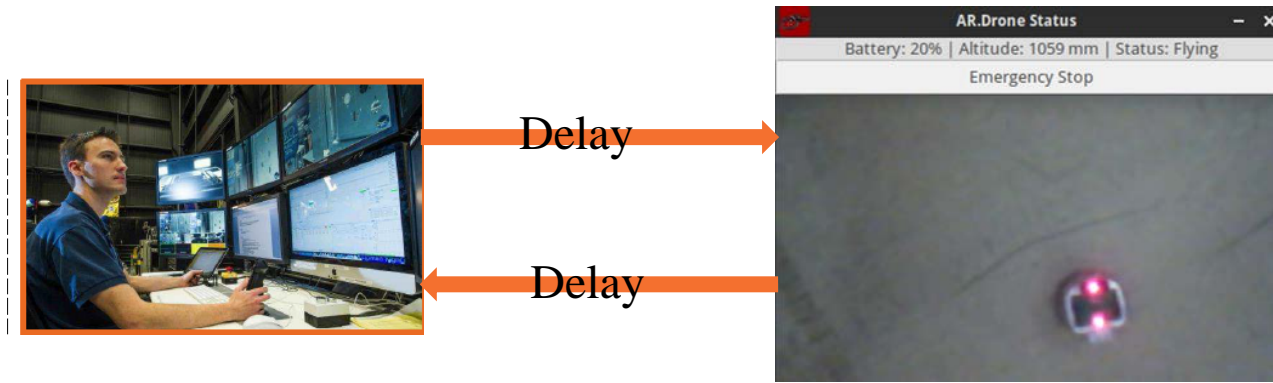
## **Trust-based Multi-Robot Symbolic Motion Planning**



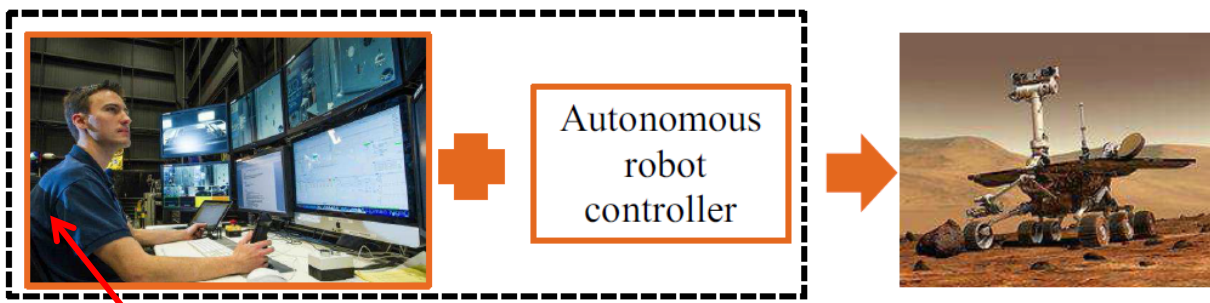
## **Conclusions**



# Tele-autonomous Operation of Mobile Robots



(Semi)autonomous Robotic Control Systems



Primary decision-maker

Milder negative effects of improper trust in mobile robotic applications

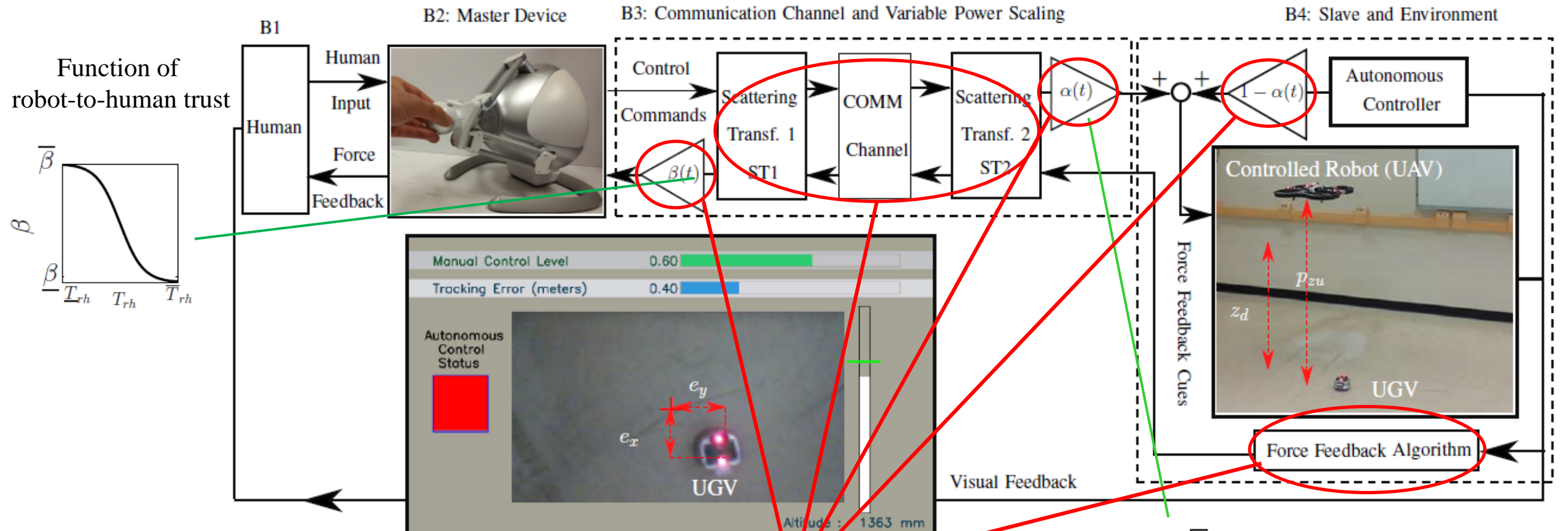


**Automated decision aids** via **objective computational trust-based measures**



# Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

[Saeidi et. al. ACC 2016; IEEE T-RO 2017; Fu et. al., ACC 2016]

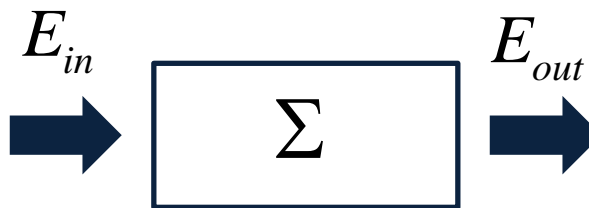


Possible sources of instability!

Passivity theory

# Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

## Passivity Theory & Port Network Theory

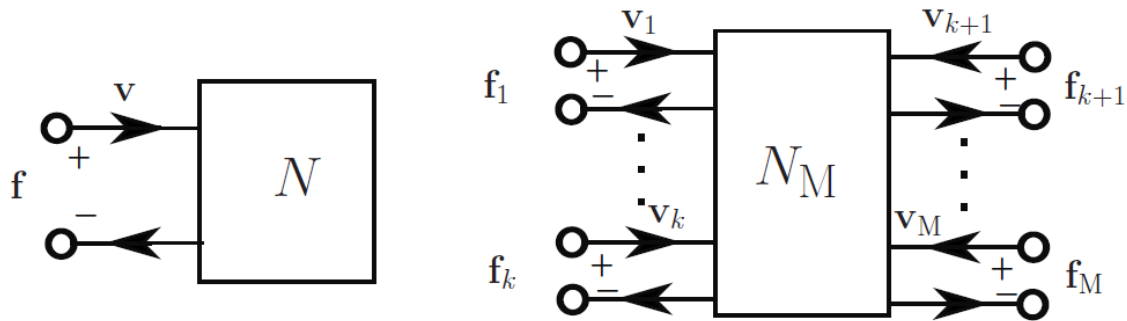


$$\Sigma: \dot{x} = f(x(t), u(t), t)$$

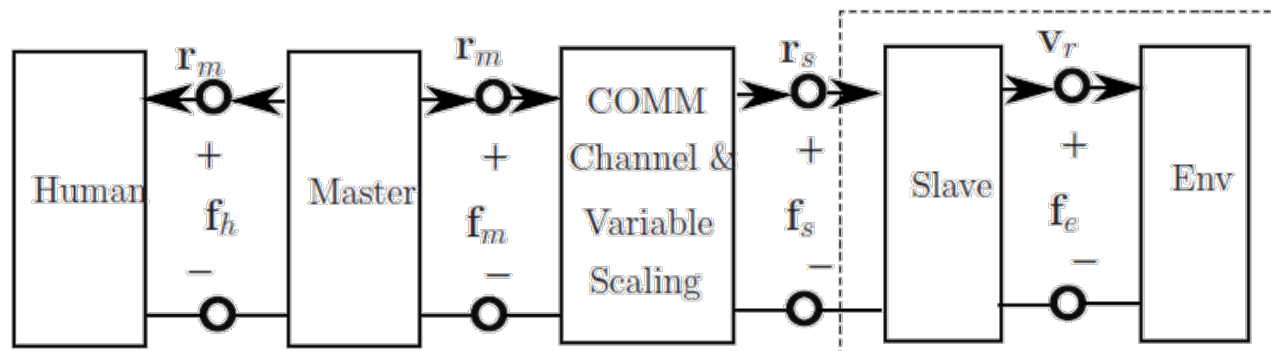
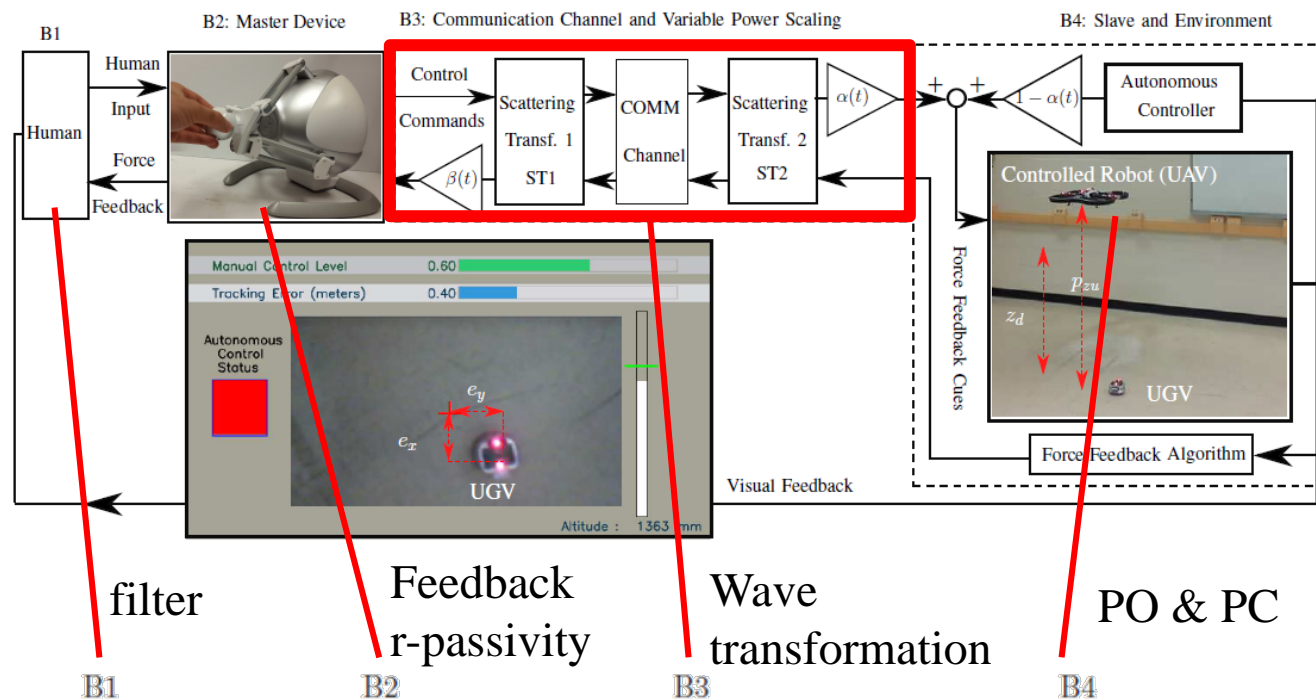
$$E_{out} \leq E_{in}$$

- Passive systems are stable
- Interconnection of passive n-ports results in a larger passive system

In teleoperation schemes force and velocities commands form the power ports



$$\int_0^t \mathbf{I}^T(\tau) \mathbf{O}(\tau) d\tau + E(0) \geq 0 \text{ must hold for } \mathbf{I}^T(t) \mathbf{O}(t) \triangleq \mathbf{v}_1^T(t) \mathbf{f}_1(t) + \dots + \mathbf{v}_M^T(t) \mathbf{f}_M(t)$$



Port-based model for the mixed-initiative bilateral haptic teleoperation

# Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

## Dynamics of the Master Haptic Device

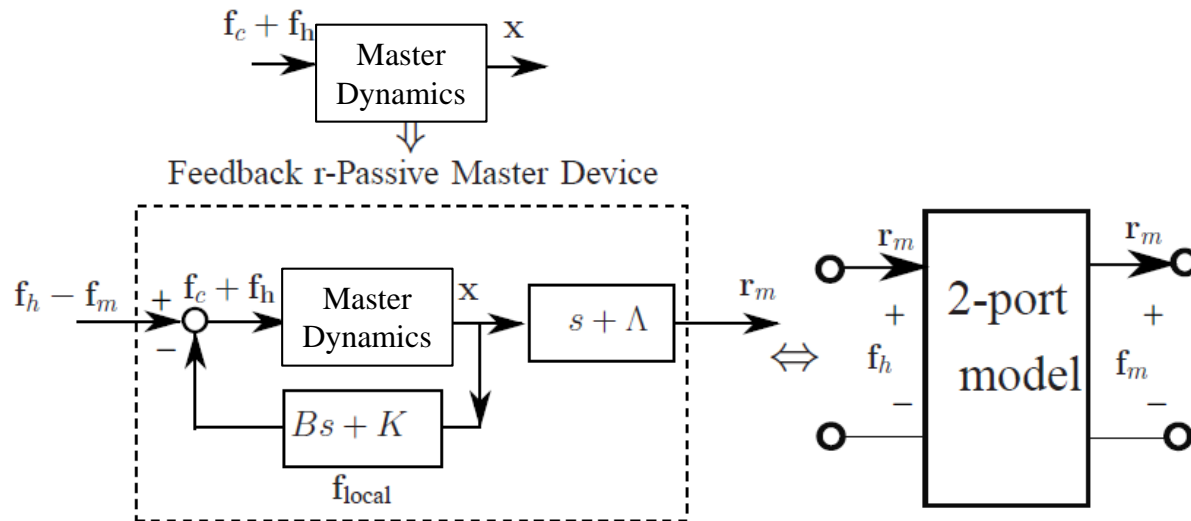
$$M(\mathbf{x})\ddot{\mathbf{x}} + C(\mathbf{x}, \dot{\mathbf{x}})\dot{\mathbf{x}} = \mathbf{f}_c + \mathbf{f}_h, \quad \mathbf{f}_c = -\mathbf{f}_{\text{local}} - \mathbf{f}_m$$

$$\mathbf{f}_{\text{local}} = B\dot{\mathbf{x}} + K\mathbf{x},$$

$$B = \text{diag}[b_1, \dots, b_n] \in \mathbb{R}^{n \times n}, b_j > 0, j = 1, \dots, n,$$

$$K = \text{diag}[k_1, \dots, k_q, 0, \dots, 0] \in \mathbb{R}^{n \times n},$$

$$k_i > 0, i = 1, \dots, q \leq n$$



## Feedback r – Passivity of the Master

$$\mathbf{r}_m = \dot{\mathbf{x}} + \Lambda\mathbf{x}$$

$$\Lambda = \text{diag}[\lambda_1, \lambda_2, \dots, \lambda_q, 0, \dots, 0] \in \mathbb{R}^{n \times n} \text{ with } \lambda_i > 0$$

$$V_{hd}(t) := \frac{1}{2} [\mathbf{r}_m^T M \mathbf{r}_m + \mathbf{x}^T (K + \Lambda B - \Lambda M \Lambda) \mathbf{x}] \geq 0$$

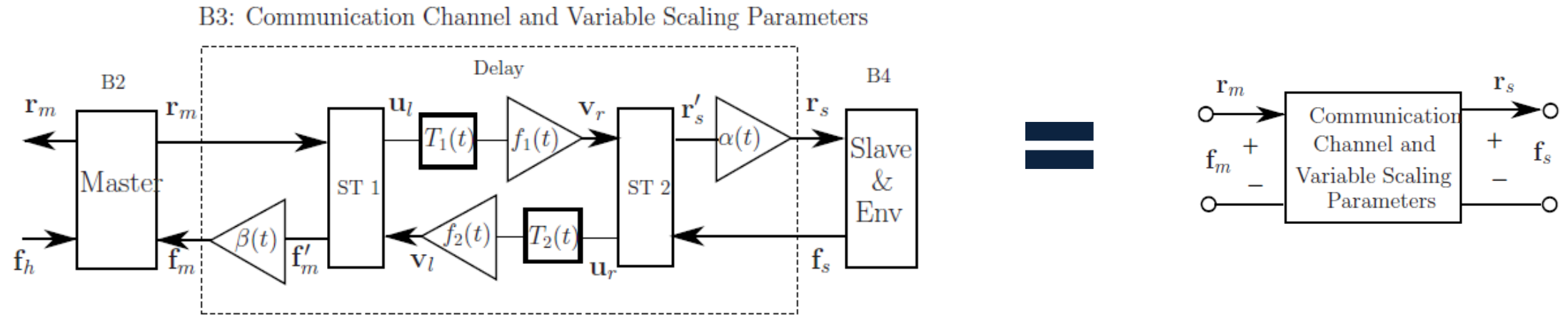
$$S_{hd}(t) := \dot{\mathbf{x}}^T [B - \frac{1}{2}(M\Lambda + \Lambda M)] \dot{\mathbf{x}} + \mathbf{x}^T \Lambda K \mathbf{x} - \mathbf{x}^T \Lambda C \dot{\mathbf{x}} \geq 0,$$

$$\mathbf{r}_m^T(t) (\mathbf{f}_h(t) - \mathbf{f}_m(t)) = \dot{V}_{hd}(t) + S_{hd}(t)$$

$$\int_0^t \mathbf{r}_m^T(\tau) (\mathbf{f}_h(\tau) - \mathbf{f}_m(\tau)) d\tau = V_{hd}(t) - V_{hd}(0) + \int_0^t S_{hd}(\tau) d\tau \geq -V_{hd}(0).$$

# Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

## Passivity of the Communication Channel with Variable Time-Delay and Variable Scaling



Block diagram for the communication channel with time-varying delays and variable power scaling

Scattering/wave transformation used to guarantee passivity  
 ( i.e.  $\int_0^t \mathbf{r}_m^T(\tau) \mathbf{f}_m(\tau) - \mathbf{r}_s^T(\tau) \mathbf{f}_s(\tau) d\tau \geq 0$  assuming  $E(0) = 0$ )

$$\mathbf{u}_l = \sqrt{\frac{\beta}{2b}} (\mathbf{f}'_m + b\mathbf{r}_m), \quad \mathbf{v}_l = \sqrt{\frac{\beta}{2b}} (\mathbf{f}'_m - b\mathbf{r}_m), \quad \mathbf{u}_r = \sqrt{\frac{\alpha}{2b}} (\mathbf{f}_s - b\mathbf{r}'_s), \quad \mathbf{v}_r = \sqrt{\frac{\alpha}{2b}} (\mathbf{f}_s + b\mathbf{r}'_s)$$

$$f_i = \sqrt{1 - \dot{T}_{i \max}}, \quad i = 1, 2, \quad b > 0: \text{Characteristic impedance}$$

$$\frac{dT_i}{dt} \leq \dot{T}_{i \max} \leq 1, \quad i = 1, 2$$

$\dot{T}_{i \max}$ : The maximum rate of increase of time-varying delay  $T_i(t)$



# Mixed-Initiative Bilateral Haptic Teleoperation of Mobile Robots based on Mutual Trust Analysis

## Passivity of the Slave using PO & PC

Passivity observer (PO):

An energy observer function

$$E_{obs}(t) = \int_0^{t^-} \mathbf{r}_s^T(\tau) \mathbf{f}_s(\tau) d\tau$$

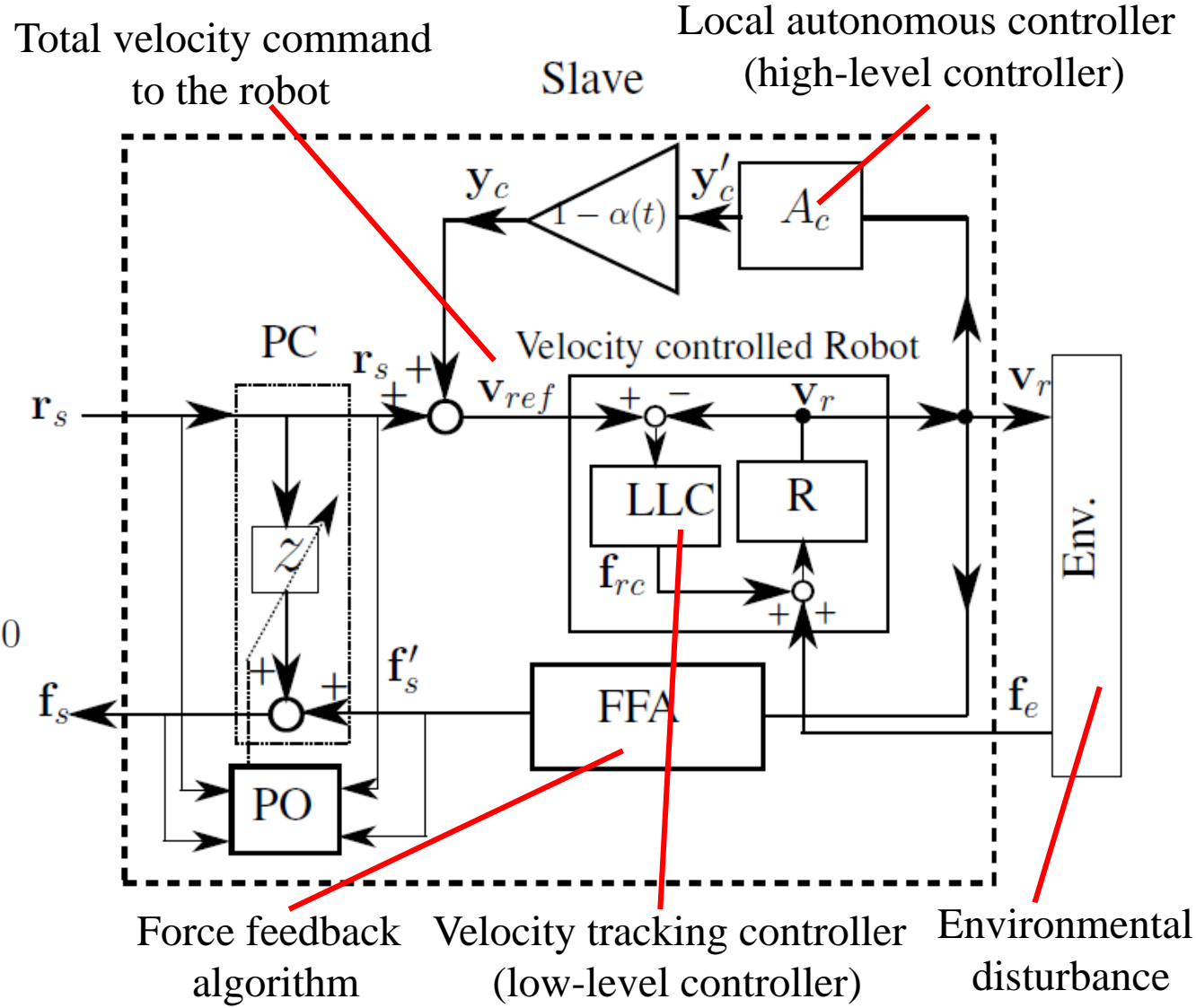
Passivity controller (PC):

a time-varying dissipation activation function

$$z(t) = \begin{cases} -\frac{\mathbf{r}_s^T(t) \mathbf{f}'_s(t)}{\|\mathbf{r}_s(t)\|_2^2} & \text{if } E_{obs}(t) = 0 \text{ \& } \mathbf{r}_s^T(t) \mathbf{f}'_s(t) < 0 \\ 0 & \text{otherwise} \end{cases}$$

$$\mathbf{f}_s(t) = \mathbf{f}'_s(t) + z(t) \mathbf{r}_s(t)$$

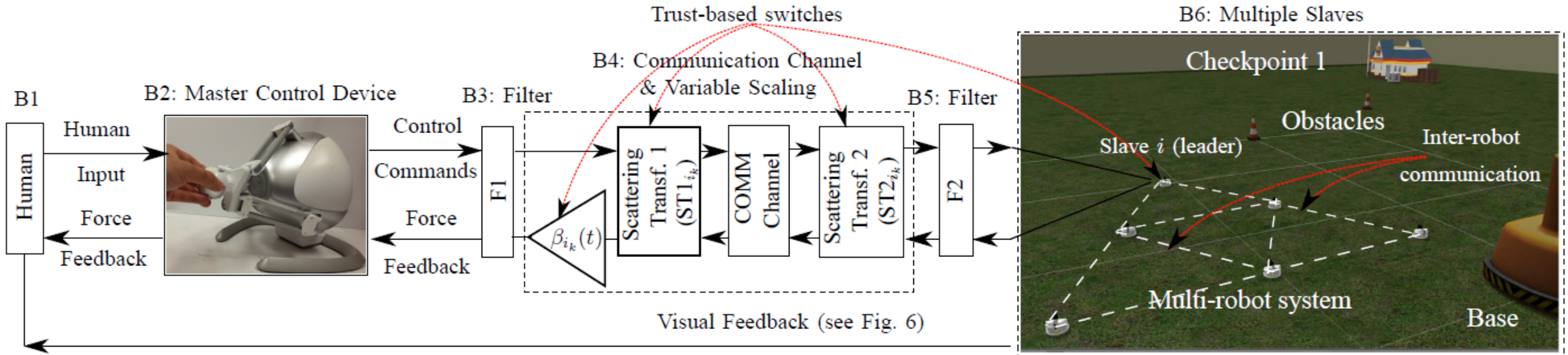
Guarantee passivity of the slave  $\int_0^t \mathbf{r}_s^T(\tau) \mathbf{f}_s(\tau) d\tau \geq 0$



# Trust-based Bilateral Teleoperation of Multi-Robot Systems [Saeidi et. al. IROS 2017]

## Motivation

- Reduced manpower for control of a robot team
- Increased robustness and flexibility of the robotic agents via cooperation



## Challenges

- Stability of the proposed scheme under the effects of switching
- Tracking performance of the system under the proposed scheme

# Passivity of Switched Systems

[Saeidi et. al. IROS 2017]

**Definition 3** [118] For systems with discontinuous supply rate, and/or switched inputs/outputs with a common storage function, the following must hold

$$\sum_{k=0}^{S-1} \left\{ \int_{t_k^+}^{t_{k+1}} \mathbf{y}_k^T(\tau) \mathbf{u}_k(\tau) d\tau \right\} + \int_{t_S^+}^t \mathbf{y}_S^T(\tau) \mathbf{u}_S(\tau) d\tau + V(0) \geq 0,$$

where  $t_k$ s are the time instants that discontinuities in the inputs and outputs or a switching of the system input and output.

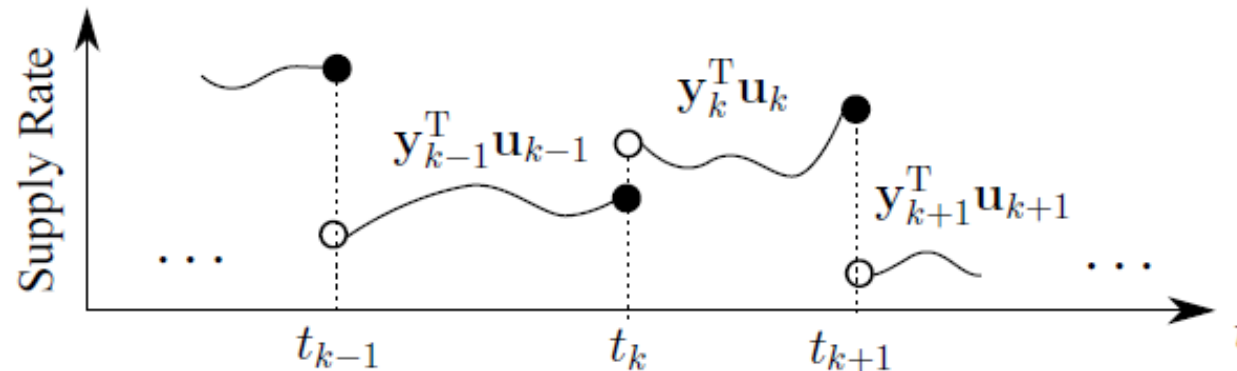
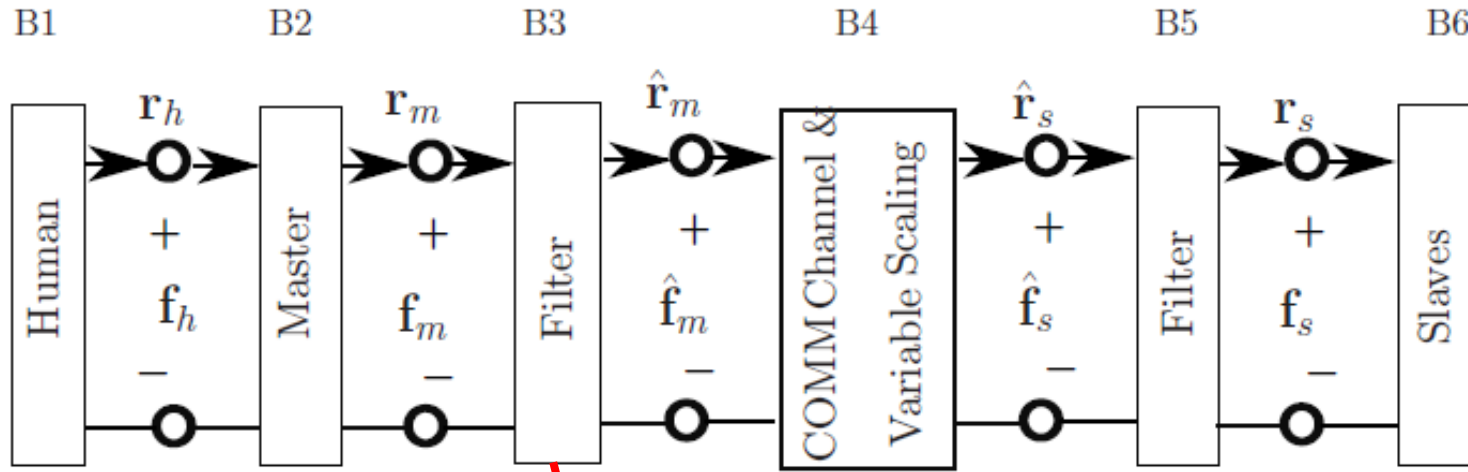


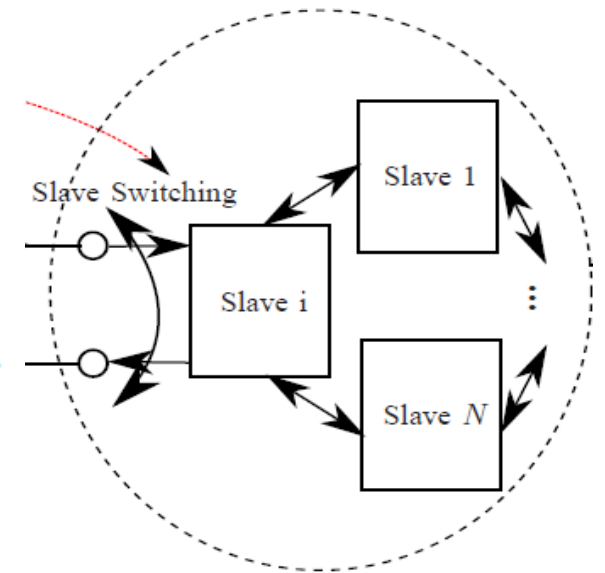
Fig. 2: Discontinuous/switched supply rate.

# Passivity of the Trust-based Bilateral Teleoperation of Multi-Robot Systems

[Saeidi et. al. IROS 2017]



- Select a leader robot with the highest trust level



$$\dot{p}(t) = (\Omega(t) - I)Lp(t) + D_{i_k}(t)r_{s_k}(t)$$

$$\delta_{i_k}(t) = \begin{cases} 1 & \text{if slave } i \text{ is the leader} \\ 0 & \text{otherwise} \end{cases}$$

$$V_{f_s}(t) = \frac{1}{2}p^T(t)Lp(t) \geq 0$$

input  $r_{s_k}(t)$

output  $f_{s_k}(t) = D_{i_k}(t)^T Lp(t)$

The relative position of the leader robot with its neighbors as haptic feedback

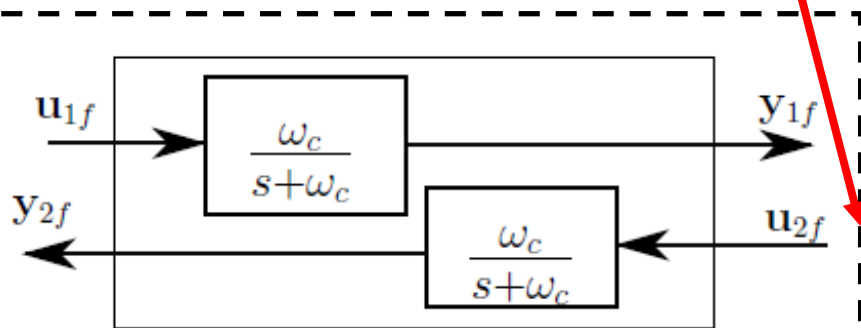


Fig. 5: Two-port filter.



## **Background and Motivation**



## **Computational Trust Models**



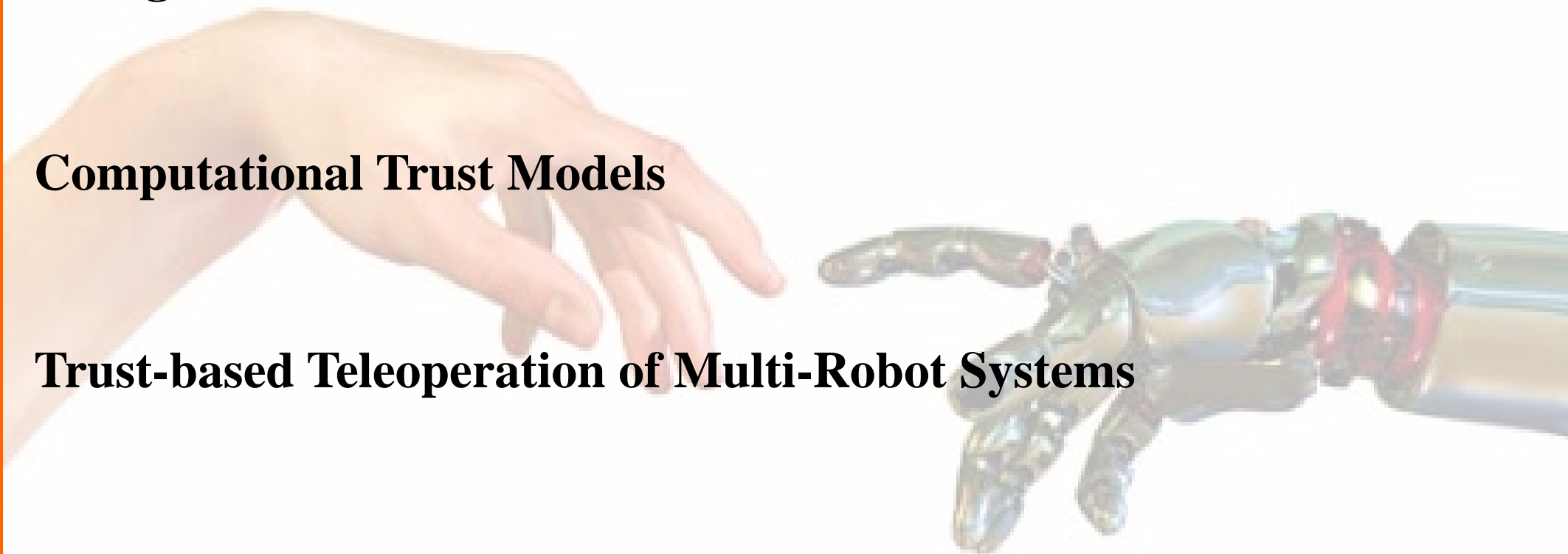
## **Trust-based Teleoperation of Multi-Robot Systems**



## **Trust-based Multi-Robot Symbolic Motion Planning**



## **Conclusions**



# Trust-based Multi-Robot Symbolic Motion Planning

## Linear Temporal Logic (LTL)

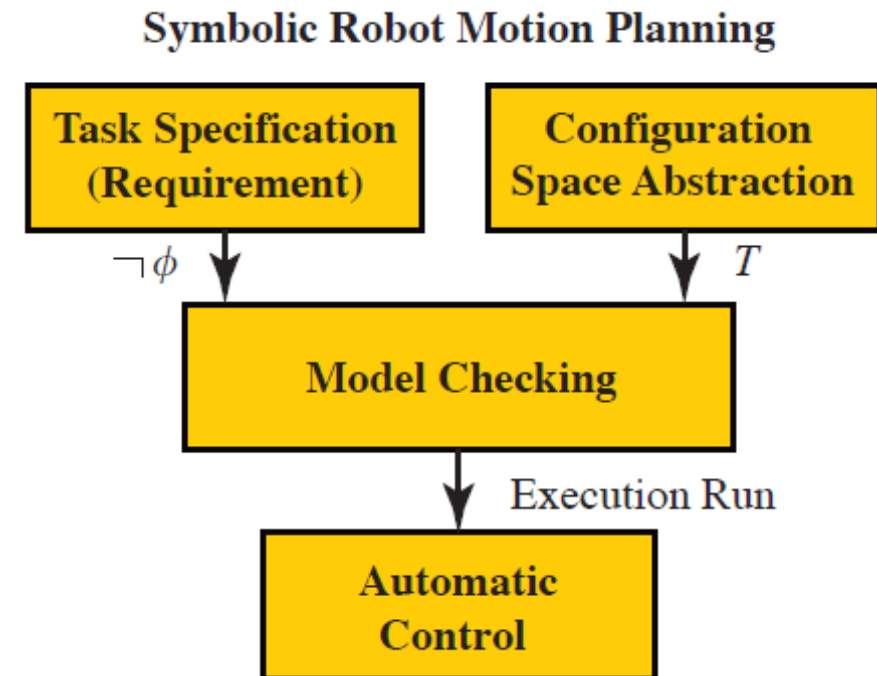
- **Propositional Operators:** negation  $\neg$ , conjunction  $\wedge$ , disjunction  $\vee$ , implication  $\rightarrow$ , equivalence  $\leftrightarrow$
- **Temporal Operators:** until  $U$ , always  $\square$ , eventually  $\diamond$
- **Expressive Motion Tasks:** Reachability (liveness)  $\diamond\pi_1$ , obstacle avoidance and safety  $\square\neg\pi_2$ , convergence (stability)  $\diamond\square\pi_1$ , sequencing and temporal ordering

## Labeled Transition System (LTS)

A transition system is a tuple  $T = (S, S_0, Act, \delta, \Pi, L)$ , where  $S$  is a set of states,  $S_0$  is a set of initial states,  $Act$  is a set of actions,  $\delta$  is a transition relation,  $\Pi$  is the set of atomic propositions, and  $L$  is a labeling function.

## Model Checking

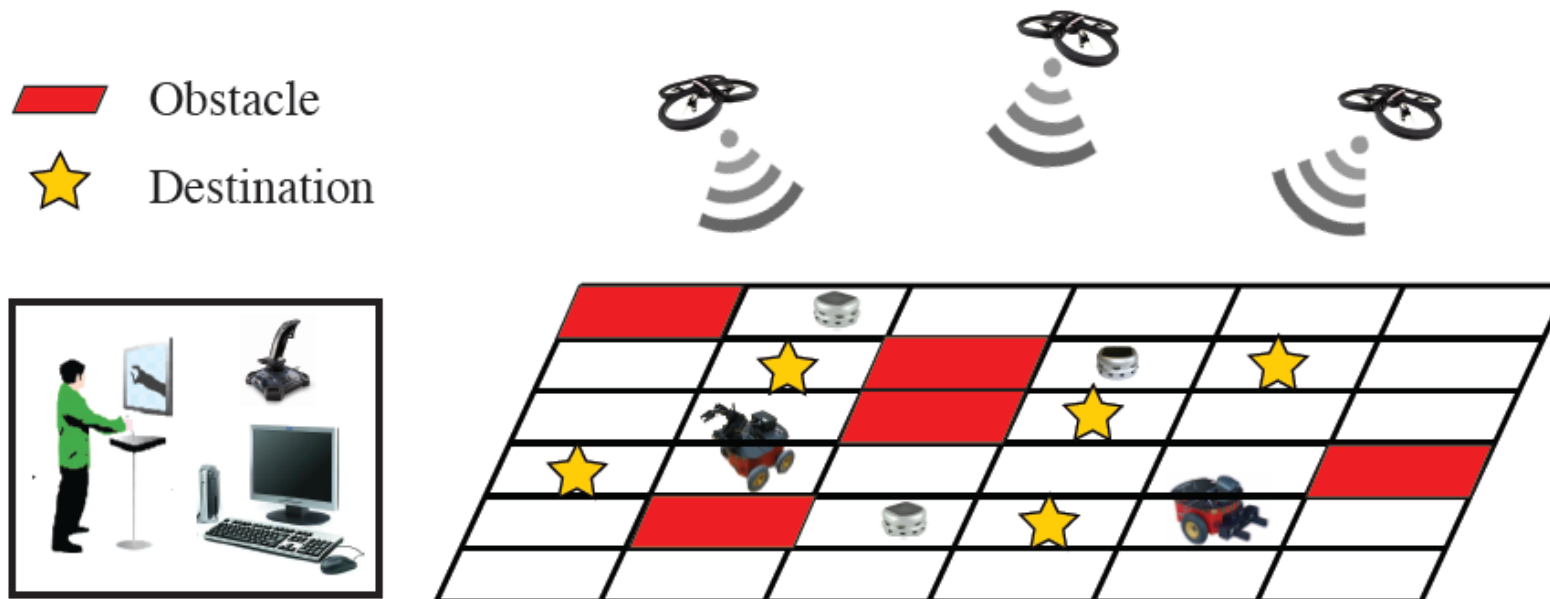
Checking whether  $T$  satisfies  $\phi$  over  $\Pi$  is called model checking. A model checker will return true if the formula is satisfied. If no such run can be found, the model checker returns a counterexample.





# Trust-based Multi-Robot Symbolic Motion Planning

[Spencer et. al., IROS 2016; Mahani and Wang, DSCC 2016; Wang et. al., ACM TiiS 2017]



## Example High-level Specification for ISR Tasks

$$\phi = \underbrace{\bigwedge_{j \in \text{Goals}} \diamond \pi_j \wedge \bigwedge_{j \in \text{Final Goals}} \diamond \square \pi_j}_{\text{Reachability}} \wedge \underbrace{\bigwedge_{j \in \text{Obs}} \square \neg \pi_j}_{\text{Obstacle Avoidance}} \wedge \underbrace{\bigwedge_{i=1}^N (\pi_i^c \wedge \pi_i^o \rightarrow \neg \pi_i^u)}_{\text{Robot Collision Avoidance}}$$

# Trust-based Multi-Robot Symbolic Motion Planning

[Spencer et. al., IROS 2016; Mahani and Wang, DSCC 2016; Wang et. al., ACM TiiS 2017]

## Trust-based Decomposition

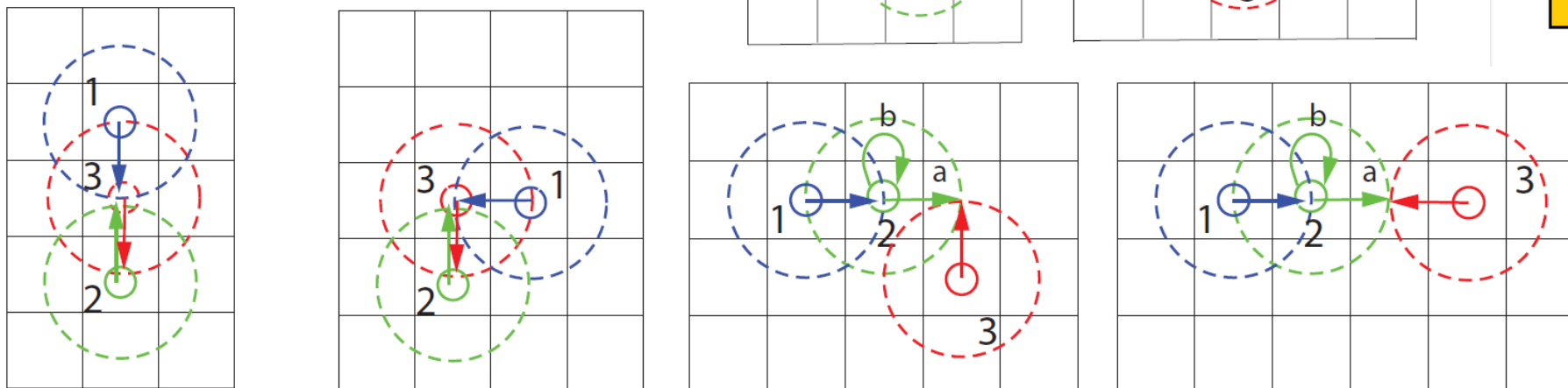
- High trust: more tasks assigned to more trusted robot
- Low trust: fewer tasks assigned to less trusted robot

## Compositional Reasoning

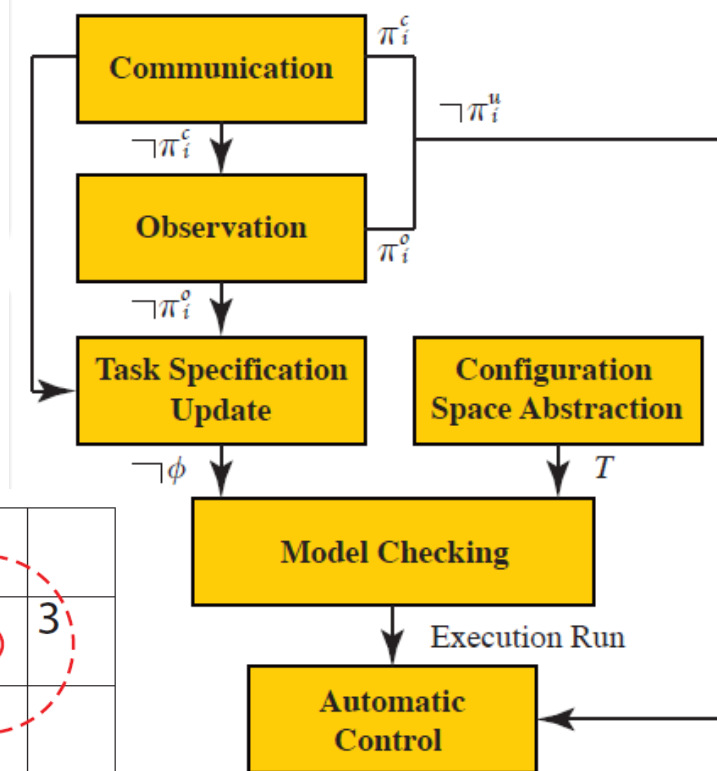
- Interleaving of transition systems
- Unconditional fairness

## Deadlock- and Livelock- Free Algorithms

- Goal destination reachability
- Inter-robot collision avoidance
- A human-in-the-loop



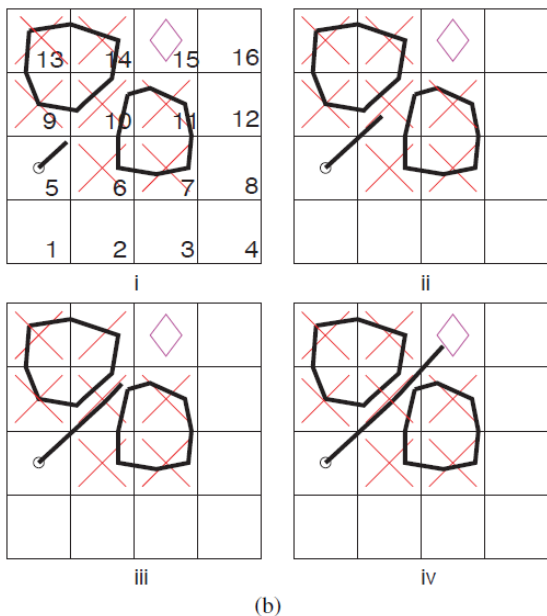
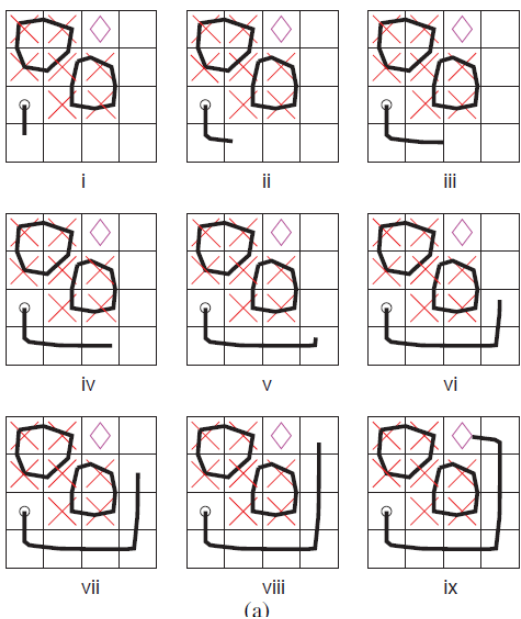
- AP for Comm, Obs, & Ctrl



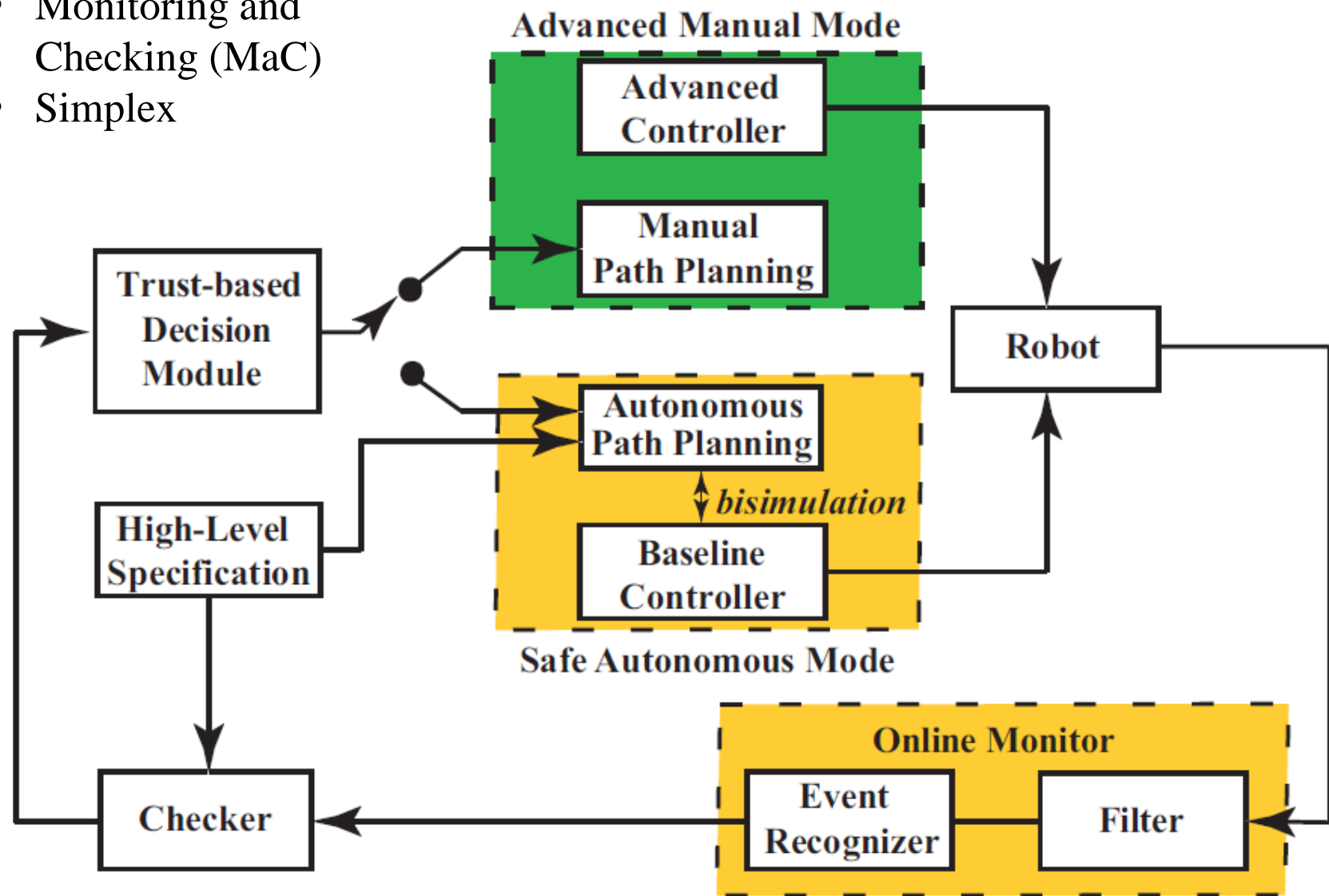
$$\bigwedge_{i=1}^N (\pi_i^c \wedge \pi_i^o \rightarrow \neg\pi_i^u)$$

# Trust-based Multi-Robot Symbolic Motion Planning

[Spencer et. al., IROS 2016; Mahani and Wang, DSCC 2016; Wang et. al., ACM TiiS 2017 ]



- Monitoring and Checking (MaC)
- Simplex





## **Background and Motivation**



## **Computational Trust Models**



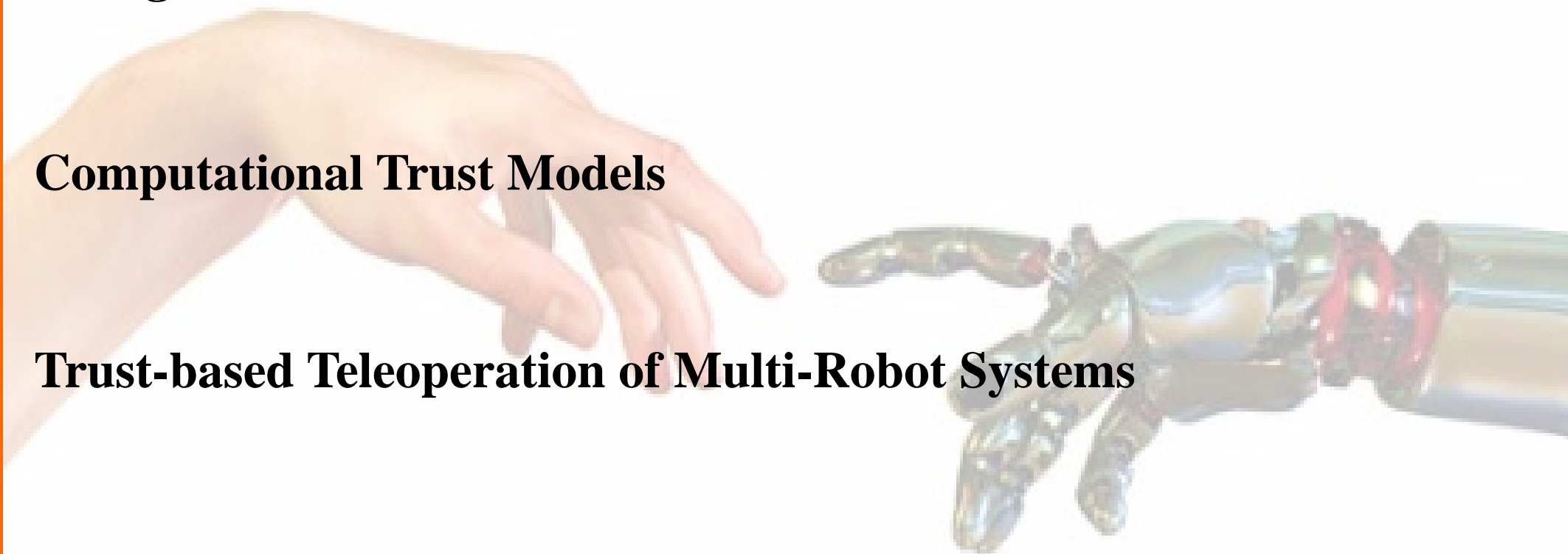
## **Trust-based Teleoperation of Multi-Robot Systems**



## **Trust-based Multi-Robot Symbolic Motion Planning**



## **Conclusions**



# Conclusions

- Computational trust models that are dynamic, quantitative, and probabilistic for real-time robotic operation
  - Human trust in robot; Robot trustworthiness; Robot trust in human; Trust propagation in multi-robot systems
- Mutual trust based bilateral teleoperation of mobile robots
  - Trust based shared control; Trust based haptic feedback; Passivity based analysis for multi-robot switches
- Trust based symbolic multi-robot motion planning with a human-in-the-loop
  - Trust based compositional reasoning for multi-robot systems; Trust based run time verification for switches between manual and autonomous motion planning





Dr. Hamed Saeidi



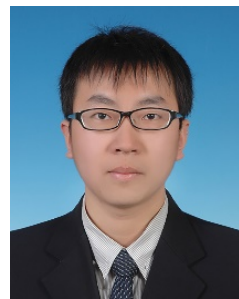
Dr. Rahman Mizanoor



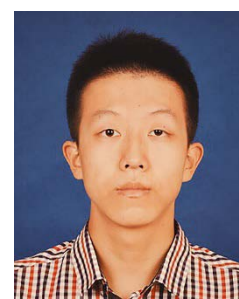
Mr. Behzad Sadr



Mr. Adam Spencer



Mr. Xiaotian Wang



Mr. Zhanrui Liao



Ms. Qiuchen Wang



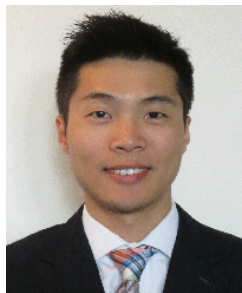
Mr. Jonathan Todd



Mr. James Svacha



Mr. Foster McLane



Mr. Longsheng Jiang



Mr. Maziar Mahani



Mr. Fangjian Li



Mr. Huanfei Zheng



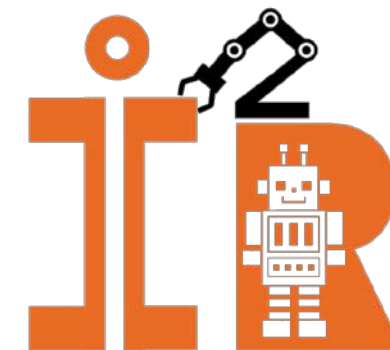
Mr. Evan Sand



Ms. Swetha Mahadevan



Mr. Sanghamitra Ahirrao



**Thank you!**



Interdisciplinary &  
Intelligence Research